

ARTICLE

Cross-sectional and confining system unification on peak compressive strength of FRP confined concrete

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Abstract

Despite the many axial confinement models already proposed for the determination of the peak compressive strength of fiber-reinforced polymer (FRP) confined concrete columns, they are, in general, applicable only to concrete columns of circular or square cross-section, with full or partial confinement arrangements. In this study, by proposing a cross-sectional and confining system unification approach, a new model is developed and calibrated based on a large test database. For the generalization of the cross-section and FRP-based confinement arrangement, the concept of confinement efficiency factor with a unified mathematical framework is adopted. By simulating experimental tests and comparing to the predictions of existing confinement models, the developed one demonstrates a very high reliability and suitable for design purposes by balancing the simplicity of the usage and accuracy.

KEYWORDS

FRP-confined concrete, partial confinement, peak compressive strength, square cross-section, unified model

1 | INTRODUCTION

In the past two decades, many studies have been conducted on the behavior of fiber-reinforced polymer (FRP) confined concrete column under uniaxial compression loadings, where the column response in terms of load-carrying and deformation capacities and energy dissipation can be upgraded proficiently, dependent on an adequate design circumstances.^{1–9}

For the case of FRP fully confined concrete columns (FFCC as illustrated in Figure 1), Valdmanis et al.¹ experimentally evidenced the reliability of full confinement arrangement in the enhancement of axial and dilation behavior, depending upon FRP volumetric ratio, where

improvements were more pronounced for normal-strength concrete columns than high-strength concrete ones. It is well-documented from experimental evidence that the application of FRP wrapping solution for circular cross-section concrete columns (FFCC) is more effective than its application for the case of square cross-section ones (FFSC in Figure 1a) due to the detrimental effect of the corner radius (r), which is generally known as shape effect induced by horizontal arching action phenomenon. Experimental studies (Shan et al.²) evidenced that by decreasing the corner radius ratio ($R_b = 2r/b$ where b is the length of section side) from one (representing a circular cross-section) to zero (representing a square cross-section with sharp edge), the efficiency of confinement strategy decreases significantly. On the other hand, since the usage of fully FRP confining configuration in real cases of strengthening might not be cost competitive, the application of a partially confining strategy can be regarded as a reliable alternative under adequate design

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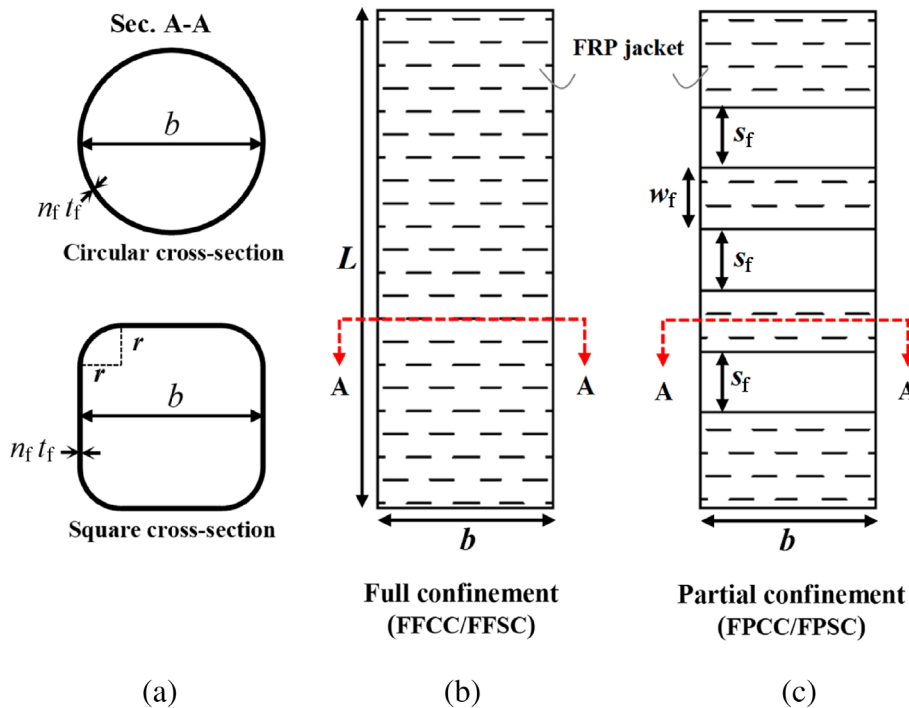


FIGURE 1 Concrete columns of (a) circular and square cross-section (CC, SC) with (b) full confinement arrangements (FFCC/FFSC), and (c) partial confinement arrangements (FPCC/FPSC)

circumstances. Barros and Ferreira³ evidenced experimentally that, although the effectiveness of FRP partial confinement system applied to circular column (FPCC in Figure 1b) is smaller than of a full confining system (FFCC) due to vertical arching action effect, a still significant level of load carrying capacity can be obtained, depending on the distance between FRP strips (S_f) and existing steel hoops. For the case of FRP partially confined square concrete elements (FPSC in Figure 1b), Guo et al.^{4,5} experimentally demonstrated that FRP thickness-induced enhancements in terms of peak axial compressive strength are quite marginal for the cases with largely spaced FRP strips.

In order to predict peak axial compressive strength (f_{cc}), a variety of confinement models has been proposed (i.e.,^{10–20}). Nonetheless, most of the models are only reliable and applicable to concrete columns of circular or square cross-section with full or partial confinement arrangements. Considering circular cross-section as a special case for square column where $R_b = 1$, and full confinement arrangement as a special case of partially confining configuration where $S_f = 0$, the reliability of these models for various confinement scenarios is, at least, arguable. Accordingly, a more-reliable model, which is inevitably established by regression analysis technique, can be calibrated/developed through cross-sectional and confining system unification. Few models generalized for FFCC, FFSC, FPCC, and FPSC have been proposed in the literature for the calculation of peak axial compressive strength (i.e., CNR DT 200/2004¹² and fib¹³).

In these models, for the purpose of unification, the concept of confinement efficiency factor is adopted to take into account the effect of vertical and horizontal arching action. Furthermore, in general, most of the existing models were calibrated by using test database with limited variables, that is, concrete properties, specimen size, corner radius ratio, and FRP confinement configuration. Consequently, statistical assessment and subsequently recalibration of these models based on a more comprehensive and larger database would be necessary for enhancing their predictive performance.

In this study, a new model is developed to predict the peak compressive strength (f_{cc}) with a unified character for FFCC, FFSC, FPCC, and FPSC under axial loading. For this purpose, a comprehensive database was compiled comprising 1528 FFCC, 308 FFSC, 171 FPCC, and 23 FPSC registered experimentally in the literature. This model adopts the concept of confinement efficiency factor for the generalization of the cross-section and confining system, which is calibrated based on the collected database. The model validation is demonstrated, and its predictive performance is compared with the one of other existing models.

2 | TEST DATABASE

To evaluate the reliability of existing models using statistical analysis, a large test database was built, including 2031 FRP confined concrete column specimens tested

TABLE 1 Summary of the compiled database for FFCC, FPCC, FFSC, and FPSC

Confinement arrangement	Number of datasets		f_{co} range (MPa)	f_{cc}/f_{co} range	L range (mm)	b range (mm)	E_f range (GPa)	ϵ_{fu} range	R_b^a	R_f^b
FFCC/FFSC/FPCC/FPSC	2031	Min.	6.6	1.0	100	50	9.5	0.004	0.00	0.00
		Max.	204.0	6.9	1200	400	657	0.100	1.00	0.75
		Mean	44.1	1.9	321.8	149.4	177.7	0.024	0.89	0.05
		CoV	0.691	0.424	0.383	0.296	0.572	0.791	0.301	2.663
rFFCC	1529	Min.	6.6	1.0	100	50	9.5	0.004	1	0
		Max.	204.0	6.9	915	305	657	0.100	1	0
		Mean	47.7	2.1	300.1	144.3	173.4	0.024	1	0
		CoV	0.701	0.417	0.352	0.295	0.614	0.801	0.000	0.000
FFSC	308	Min.	8.7	1.0	280	100	9.5	0.009	0.00	0
		Max.	77.2	4.3	1200	400	259.7	0.093	0.80	0
		Mean	33.3	1.6	394.1	168.9	166.8	0.027	0.31	0
		CoV	0.411	0.353	0.402	0.306	0.571	0.799	0.675	0.000
FPCC	171	Min.	16.6	1.0	200	100	104.6	0.015	1	0.05
		Max.	101.2	3.1	700	300	259.7	0.019	1	0.75
		Mean	33.5	1.5	353.5	154.9	230.9	0.017	1	0.33
		CoV	0.436	0.284	0.321	0.214	0.153	0.080	0.000	0.542
FPSC	23	Min.	12.3	1.0	500	150	73.0	0.015	0.13	0.10
		Max.	34.7	1.4	750	200	259.7	0.028	0.33	0.51
		Mean	28.3	1.22	557.4	183.4	215.7	0.020	0.30	0.24
		CoV	0.287	0.092	0.152	0.107	0.264	0.172	0.129	0.434

^a $R_b = 2r/b$ where r is the corner radius of the cross-section; b is the cross-section dimension as shown in Figure 1.

^b $R_f = s_f/b$ where s_f is the distance between two adjacent strips as shown in Figure 1.

Abbreviations: CoV, coefficient of variation; FFCC, FRP fully confined concrete columns; FFSC, FRP fully confined square cross-section; FPCC, FRP partial confinement system applied to circular column; FPSC, FRP partially confined square concrete elements; FRP, fiber-reinforced polymer; max., maximum; min., minimum.

under axial compressive loading. This database includes 1528 fully confined specimens of circular cross-section (FFCC), 308 fully confined specimens of square cross-section (FFSC), 171 partially confined specimens of circular cross-section (FPCC), and 23 partially confined specimens of square cross-section (FPSC). Specimens in the following conditions were not included in the database: (i) having internal transverse and longitudinal steel reinforcements; (ii) having helicoidal FRP wrapping confinement configurations; (iii) with incomplete information, such as mechanical properties of the intervenient materials; (iv) with premature FRP debonding; (v) with hybrid confining systems (application of different FRP sheets) for the confinement; (vi) under eccentric axial loading; (vii) with a peak strength less than the one of its unconfined counterpart.

Table 1 presents the details of the assembled database of FFCC, FPCC, FFSC, and FPSC with a wide range of key parameters. As shown, the axial compressive strength of unconfined concrete (f_{co}) varies from

6.6 to 240 MPa with the mean and coefficient of variation (CoV) values of 44.1 and 0.69 MPa, respectively. The confinement-induced improvement (f_{cc}/f_{co}) is in the range of 1.0–6.9 with mean and CoV of 1.9 and 0.424, respectively. The diameter of the circular columns or cross-section edge width (b) varies from 50 to 400 mm with the mean and CoV values of 149 and 0.296 mm, respectively. The height of the column specimens (L) varies from 100 to 1200 mm with the mean and CoV values of 322 and 0.383 mm, respectively. The database comprises specimens wrapped with carbon (CFRP), basalt, aramid, glass, polyethylene naphthalate, and polyethylene terephthalate (PET) fibers. The elastic modulus of the confining FRP (E_f) is in the range of 9.5–657 GPa with the mean and CoV values of 177.7 and 0.572 MPa, respectively. The ultimate tensile strain (ϵ_{fu}) varies between 0.004 and 0.10 with mean and CoV of 0.024 and 0.791, respectively. For the case of partial confinement configuration, the database covers test specimens with various R_f and s_f/b ranging from 0.05 to

TABLE 2 Existing strength models for FRP confined concrete columns

ID	Model expression	Model parameters	Applicability
fib ¹³	$\frac{f_{cc}}{f_{co}} = 1 + 3.3 \frac{f_{l,rupt}}{f_{co}}$ for $\frac{f_{l,rupt}}{f_{co}} \geq 0.07$	$f_{l,rupt} = 2k_h k_v \frac{n_f t_f E_f}{b} \epsilon_{h,rupt}$ for $n_f \leq 3$	FFCC
	$\frac{f_{cc}}{f_{co}} = 1$ for $\frac{f_{l,rupt}}{f_{co}} \leq 0.07$	$f_{l,rupt} = 2k_h k_v \frac{n_f^{0.85} t_f E_f}{b} \epsilon_{h,rupt}$ for $n_f \geq 4$	FFSC FPCC FPSC
CNR DT 200/2004 ¹²	$\frac{f_{cc}}{f_{co}} = 1 + 2.6 \left(\frac{f_{l,rupt}}{f_{co}}\right)^{\frac{2}{3}}$ for $\frac{f_{l,rupt}}{f_{co}} \geq 0.05$	$f_{l,rupt} = \frac{1}{2} k_h k_v \rho_f E_f \epsilon_{fd,rid}$	FFCC
	$\frac{f_{cc}}{f_{co}} = 1$ for $\frac{f_{l,rupt}}{f_{co}} \leq 0.05$	$\rho_f = \frac{4n_f t_f}{b}$ for FFCC/FFSC $\rho_f = \frac{4n_f t_f w_f}{s_f b}$ for FPCC/FPSC	FFSC FPCC FPSC
Guo et al. ^{4,5}	$\frac{f_{cc}}{f_{co}} = 1 + 2(\rho_{Ke} - 0.01)\rho_e$ for $\rho_{Ke} \geq 0.01$	$\rho_{Ke} = 2k_v \frac{n_f t_f E_f \epsilon_{co}}{b f_{co}}$ for FFCC/FPCC	FFCC
	$\frac{f_{cc}}{f_{co}} = 1$ for $\rho_{Ke} \leq 0.01$	$\rho_{Ke} = 2k_h k_v \frac{n_f t_f E_f \epsilon_{co}}{\sqrt{2} b f_{co}}$ for FFSC/FPSC	FFSC FPCC FPSC
ACI 440.2R-17 ¹⁴	$\frac{f_{cc}}{f_{co}} = 1 + 3.3 \psi_f \frac{f_{l,rupt}}{f_{co}}$ for $\frac{f_{l,rupt}}{f_{co}} \geq 0.08$	$f_{l,rupt} = 2 \frac{n_f t_f E_f}{b} \epsilon_{h,rupt}$ for FFCC	FFCC
	$\frac{f_{cc}}{f_{co}} = 1$ for $\frac{f_{l,rupt}}{f_{co}} \leq 0.08$	$f_{l,rupt} = 2k_h \frac{n_f t_f E_f}{\sqrt{2} b} \epsilon_{h,rupt}$ for FFSC	FFSC
Fallahpour et al. ¹⁵	$\frac{f_{cc}}{f_{co}} = 1 + (2.5 - 0.01 f_{co}) \frac{f_{l,u}}{f_{co}}$	$f_{l,u} = 2 \frac{n_f t_f E_f}{b} \epsilon_{fu}$	FFCC
Wei and Wu ¹⁶	$\frac{f_{cc}}{f_{co}} = 1 + 2.2 \left(\frac{2r}{b}\right)^{0.72} \left(\frac{f_{l,u}}{f_{co}}\right)^{0.94}$	$f_{l,u} = 2 \frac{n_f t_f E_f}{b} \epsilon_{fu}$	FFCC FFSC
	Nistico and Monti ¹⁷	$\frac{f_{cc}}{f_{co}} = 1 + 2.2 \left(\frac{2r}{b}\right) \frac{f_{l,u}}{f_{co}}$	$f_{l,u} = 2 \frac{n_f t_f E_f}{b} \epsilon_{fu}$
Cao et al. ¹⁸	$\frac{f_{cc}}{f_{co}} = 1 + 8.34 \left(\frac{K_L}{E_c}\right)^{1.03} \left(\frac{2r}{b}\right)^{0.81} \left(\frac{30}{f_{co}}\right)^{0.54} \left(\frac{\epsilon_{fu}}{\epsilon_{co}}\right)^{0.82}$	$K_L = \frac{2n_f t_f E_f}{b}$	FFCC
		$E_c = 4730 \sqrt{f_{co}}$ $\epsilon_{co} = 0.000937 f_{co}^{0.25}$	FFSC
Lin et al. ¹⁹	$\frac{f_{cc}}{f_{co}} = 1 + 2.2 \lambda f_{co}^{0.11} \left(\frac{f_{l,rupt}}{f_{co}}\right)^{0.81}$	$f_{l,rupt} = 2 \frac{n_f t_f E_f}{b} \epsilon_{h,rupt}$	FFCC
		$\lambda = 13.2 f_{co}^{-0.95} f_{l,u}^{0.2} \leq 1$ $f_{l,u} = 2 \frac{n_f t_f E_f}{b} \epsilon_{fu}$ $\epsilon_{h,rupt} = 0.74 \epsilon_{fu}$	

Note: where f_{cc} , peak axial strength of FRP confined concrete; f_{co} , axial strength of unconfined concrete; $f_{l,rupt}$ = confinement pressure corresponding to FRP rupture strain ($\epsilon_{h,rupt}$); $f_{l,u}$, confinement pressure corresponding to FRP ultimate tensile strain (ϵ_{fu}); n_f , number of FRP layers; t_f , nominal FRP thickness; k_h , confinement efficiency factor reflecting the effect of horizontal arching action; k_v , confinement efficiency factor reflecting the effect of vertical arching action; ρ_f , FRP reinforcement ratio; ρ_{Ke} , FRP confinement stiffness index; ρ_e , FRP strain ratio; ϵ_{co} , axial strain corresponding to f_{co} ; ψ_f , reduction factor recommended as 0.95; K_L , FRP confinement stiffness per the length of section dimension; E_c , concrete modulus of elasticity.

Abbreviations: FFCC, FRP fully confined concrete columns; FFSC, FRP fully confined square cross-section; FPCC, FRP partial confinement system applied to circular column; FPSC, FRP partially confined square concrete elements; FRP, fiber-reinforced polymer.

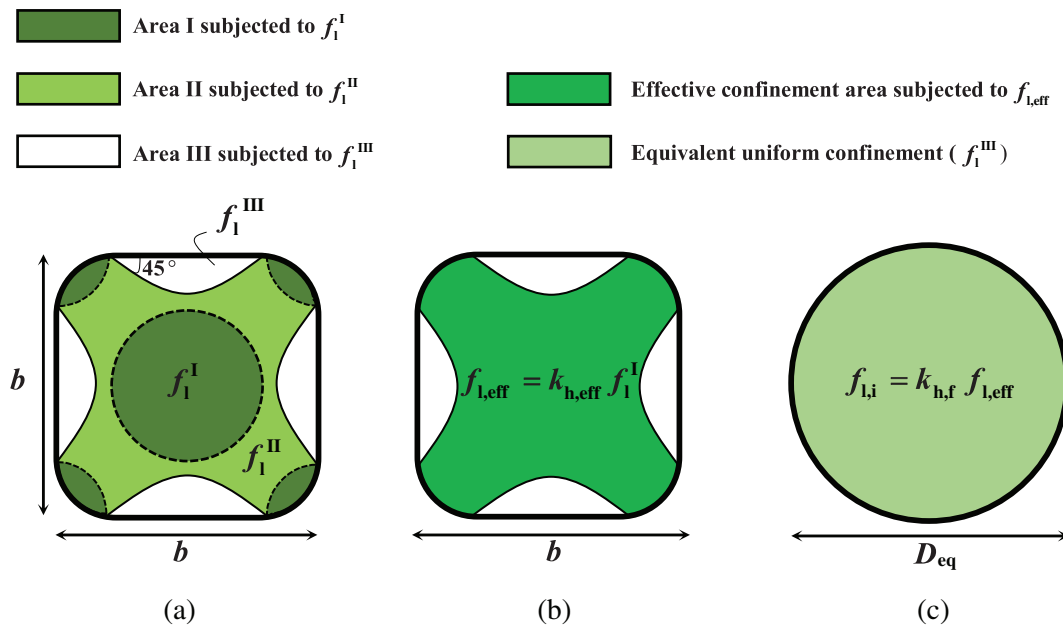


FIGURE 2 Distribution of confinement pressure within a square cross-section

0.75. For the case of square cross-section column specimens, the corner radius ratio varies from 0.0 to 0.8.

3 | EXISTING MODELS

Table 2 represents the existing models developed for the prediction of peak axial strength of FRP confined concrete. These models adopted different methodologies for developing/calibrating their performance in terms of the normalized peak axial strength (f_{cc}/f_{c0}). The formulations of these models can be generally classified into four categories based on: (i) the relation of f_{cc}/f_{c0} and the normalized confinement pressure corresponding to FRP rupture ($f_{l,rupt}/f_{c0}$)^{13,14}; (ii) the relation of f_{cc}/f_{c0} and the normalized confinement pressure corresponding to the FRP ultimate tensile strain ($f_{l,u}/f_{c0}$)¹⁵⁻¹⁷; (iii) the development of a relation in which f_{cc}/f_{c0} is as a function of the normalized confinement stiffness ($\rho_K = f_{l,rupt} \epsilon_{c0} / f_{c0} \epsilon_{h,rupt}$ where ϵ_{c0} is the axial strain corresponding to f_{c0} ; $\epsilon_{h,rupt}$ is the FRP hoop strain corresponding to rupture) and FRP strain ratio ($\rho_\epsilon = \epsilon_{h,rupt} / \epsilon_{c0}$)^{4,5}; (iv) the development of a regression-based relation in which f_{cc}/f_{c0} is determined based on the best-fit with respect to key parameters.¹⁸ Among these models, few ones^{4,5,12-14} were developed with a unified character for all FFCC, FFSC, FPCC, and FPSC cases based on the confinement efficiency factor (k_h and k_v) reflecting the effect of horizontal and vertical arching actions. The models developed by^{14,16-18} are applicable to FFCC and FFSC through cross-section

unification (i) by using k_h ¹⁴ or (ii) by empirically modeling the shape effect according to corner radius ratio (R_b).¹⁶⁻¹⁸

4 | PROPOSED MODEL

In this section, a new model is proposed for the determination of f_{cc} based on cross-sectional and confining system unification approach. The procedure to establish the unified model is briefly presented as follows:

- i. Adopting the concept of equivalent circular cross-section to convert a square into a circular column's cross-section;
- ii. Adopting the concept of confinement efficiency factor to reflect the effect of arching action phenomenon in both transversal and longitudinal directions of the column;
- iii. Establishment of the relation between normalized peak axial strength (f_{cc}/f_{c0}) with respect to normalized equivalent confinement pressure corresponding to FRP rupture stage ($f_{l,rupt}/f_{c0}$).

In this study, the diameter of the equivalent circular column (D_{eq}) is determined based on the *fib*'s¹³ recommendation where D_{eq} is assumed equal to the section dimension b (Figure 1) for the case of square cross-section ($D_{eq} = b$).

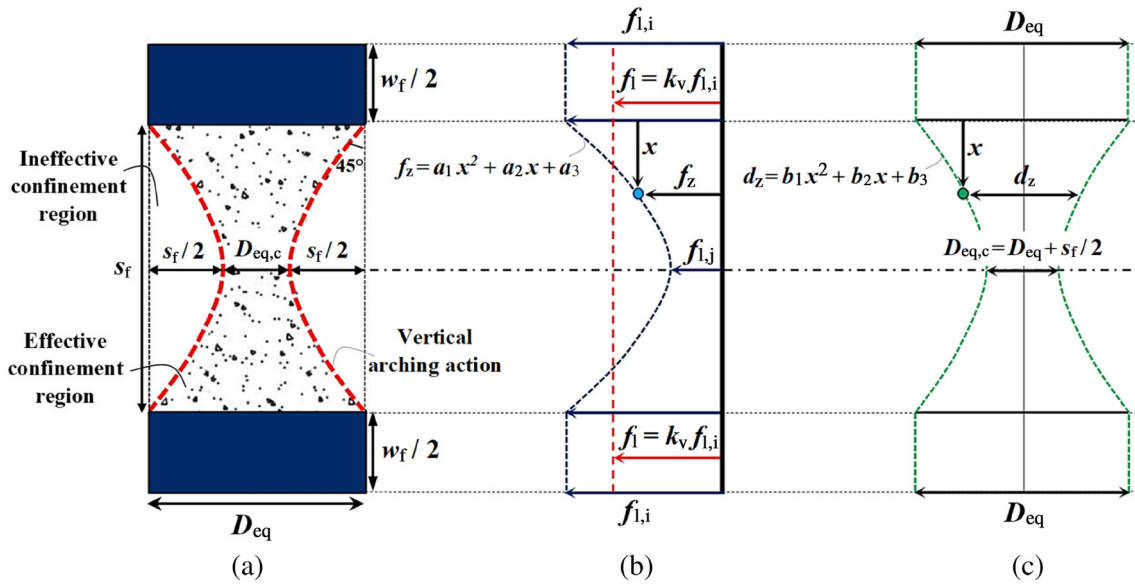


FIGURE 3 Vertical arching action phenomenon for partially FRP confined concrete

4.1 | Concept of confinement efficiency factor

For the simulation of the effect of vertical and horizontal arching actions, due to the presence of ineffective confinement regions, the concept of confinement efficiency factor is followed. By using this concept, the entire cross-section can be considered as effectively and uniformly confined at longitudinal and transversal directions. Based on experimental observations and finite element simulations, Shayanfar et al.²¹ proposed a new model to formulate the effect of horizontal arching action on the determination of the equivalent confinement pressure. As shown in Figure 2a, the original square cross-section was assumed to be subjected to three distinct levels of the confinement pressure:

- i. Area III under the lowest confinement level, which was assumed to be marginal ($f_1^{III} = 0$);
- ii. Area II under a moderate level of confinement pressure (f_1^{II}), which was assumed equal to $f_1^{II} = 0.5(f_1^I + f_1^{III}) = 0.5f_1^I$;
- iii. Area I under the highest level of confinement pressure (f_1^I).

Based on equilibrium of lateral forces in the equivalent circular cross-section, Shayanfar et al.²¹ recommended the highest level of confinement pressure (f_1^I) as follows:

$$f_1^I = 2 \frac{w_f n_f t_f}{(w_f + s_f) D_{eq}} E_f \epsilon_h \quad (1)$$

where n_f is the number of FRP layers per strip; t_f is the nominal thickness of a FRP layer; E_f is the FRP modulus of elasticity. In Figure 2b, $f_{1,eff}$ defines the effective confinement pressure uniformly acting on the region out of the parabolas (Areas I and II), which was considered proportional to f_1^I , dependent on the reduction factor $k_{h,eff}$. Consequently, by using $k_{h,eff}$, the stress field within the confined Areas I and II is converted to an effective confinement pressure ($f_{1,eff}$) uniformly distributed in these areas. Assuming $k_{h,eff}$ on the interval 0.5 and 1 corresponding to the cases of $R_b = 0$ and $R_b = 1$, respectively, Shayanfar et al.²¹ suggested this reduction factor as:

$$k_{h,eff} = 0.5(1 + 2R_b - R_b^2) \quad (2)$$

Figure 2c shows that using another reduction factor $k_{h,f}$, the effective confinement pressure ($f_{1,eff}$) can be distributed on the entire equivalent circular cross-section, leading to the uniform confinement pressure ($f_{1,i} = k_{h,f} f_{1,eff} = k_{h,f} k_{h,eff} f_1^I$). Adopting the concept of the equivalent circular section to convert Area I and Area II into an equivalent circular core with a diameter $D_{eq,c}$, Shayanfar et al.²¹ suggested this reduction factor to be dependent on R_b as:

$$k_{h,f} = \frac{D_{eq,c}}{D_{eq}} \simeq 1.17R_b - 0.46R_b^2 + 0.29 \quad (3)$$

Accordingly, by defining the confinement efficiency factor (k_h) due to horizontal arching action as $k_{h,f} k_{h,eff}$, it can be determined as:

$$k_h = k_{h,f} k_{h,eff} = 0.5(1 + 2R_b - R_b^2)(1.17R_b - 0.46R_b^2 + 0.29) \quad (4)$$

which can be simplified to:

$$k_h \simeq 0.15 + 0.93R_b \leq 1 \quad (5)$$

without significant loss of accuracy. Accordingly, by using k_h , the equivalent uniform confinement pressure acting on the entire section can be expressed as:

$$f_{l,i} = k_h f_1^I = 2k_h \frac{w_f n_f t_f}{(w_f + s_f) D_{eq}} E_f \varepsilon_h \quad (6)$$

On the other hand, for the case of partial confinement, Shayanfar et al.²² proposed a new reduction factor, k_v , for simulating the effect of vertical arching action due to the non-uniform distribution of actual confinement pressure imposed to the concrete along the column height as illustrated in Figure 3. In this figure, f_z and d_z are the distribution function of the confinement pressure and the diameter of the effective confinement region at the clear distance of x from the strip, induced by vertical arching action phenomenon. As shown, owing to vertical arching action, the strip region was assumed to be subjected to the highest confinement pressure ($f_{l,i}$), whereas the concrete at the mid-height of two consecutive strips is subjected to lowest confinement pressure ($f_{l,j}$). The average level of confinement pressure uniformly acting along the column height (f_i) can be defined as $f_i = k_v f_{l,i}$, in the compliance with the concept of confinement efficiency factor.^{23,24}

Accordingly, based on the equilibrium of confinement forces, Shayanfar et al.²² determined k_v as:

$$k_v = \frac{f_{l,i} w_f D_{eq} + 2 \int_0^{s_f/2} f_z d_z dx}{f_{l,i} (s_f + w_f) D_{eq}} = \frac{w_f + s_f \left(1 - \frac{s_f}{D} + 0.43 \left(\frac{s_f}{D}\right)^2 - 0.07 \left(\frac{s_f}{D}\right)^3\right)}{w_f + s_f} \quad (7)$$

which can be simplified without significant loss of accuracy to:

$$k_v = \frac{w_f + s_f \exp(-0.973R_f)}{w_f + s_f} \leq 1 \quad (8)$$

where $R_f = s_f/D_{eq}$. As a result, both components of the confinement efficiency factor, k_h and k_v can be calculated by using Equation (5) and Equation (8), with the design framework. Hence, for the case of partially FRP confined square concrete column (FPSC), considering $f_1 = k_v f_{l,i}$,

the confinement pressure uniformly imposed to the concrete can be determined using Equation (6) (Figure 3b):

$$f_1 = k_v f_{l,i} = 2k_v k_h \frac{w_f n_f t_f}{(w_f + s_f) D_{eq}} E_f \varepsilon_h \quad (9)$$

4.2 | Establishment of peak axial strength

This section addresses the determination of the f_{cc} corresponding to the equivalent confinement pressure at the FRP rupture ($f_{l,rupt}$). By defining $\varepsilon_{h,rupt}$ as FRP rupture strain, the $f_{l,rupt}$ can be calculated based on Equation (9) by considering $D_{eq} = b$:

$$f_{l,rupt} = 2k_v k_h \frac{w_f n_f t_f}{(w_f + s_f) b} E_f \varepsilon_{h,rupt} \quad \text{for } n_f \leq 3 \quad (10a)$$

$$f_{l,rupt} = 2k_v k_h \frac{w_f n_f^{0.85} t_f}{(w_f + s_f) b} E_f \varepsilon_{h,rupt} \quad \text{for } n_f \geq 4 \quad (10b)$$

where k_h and k_v can be calculated by Equation (5) and Equation (8), respectively. In Equation (10b), for the case with many FRP layers ($n_f \geq 4$), *fib*¹³ recommendation was followed in order to consider the decrease of FRP jacket confinement effectiveness with the increase of the FRP stiffness above a certain limit. By performing regression analysis on a large test database, Shayanfar et al.²⁵ improved the formulation suggested by Lam and Teng,²⁰ where the effects of f_{c0} and FRP ultimate tensile strain (ε_{fu}) were considered:

$$\varepsilon_{h,rupt} = \left(\frac{0.586}{0.82 + 0.23 f_{c0} \varepsilon_{fu}} \right) \varepsilon_{fu} \geq 0.35 \varepsilon_{fu} \quad (11)$$

In this study, based on the best-fit of the model with the experimental results in the database, as demonstrated in Table 1, a new relation generalized for FFCC, FFSC, FPCC, and FPSC is proposed to calculate f_{cc} , as a function of the normalized confinement pressure ($f_{l,rupt}/f_{c0}$):

$$\frac{f_{cc}}{f_{c0}} = 1 + \frac{3.4}{k_r} \left(\frac{f_{l,rupt}}{f_{c0}} \right) \quad \text{for } \frac{f_{l,rupt}}{f_{c0}} \geq 0.05 \quad (12a)$$

$$\frac{f_{cc}}{f_{c0}} = 1 \quad \text{for } \frac{f_{l,rupt}}{f_{c0}} < 0.05 \quad (12b)$$

In Equation (12a and 12b), when $f_{l,rupt}/f_{c0}$ is lower than 0.05, the confinement-induced improvement is neglected. The reduction factor k_r (larger than 1) is proposed to

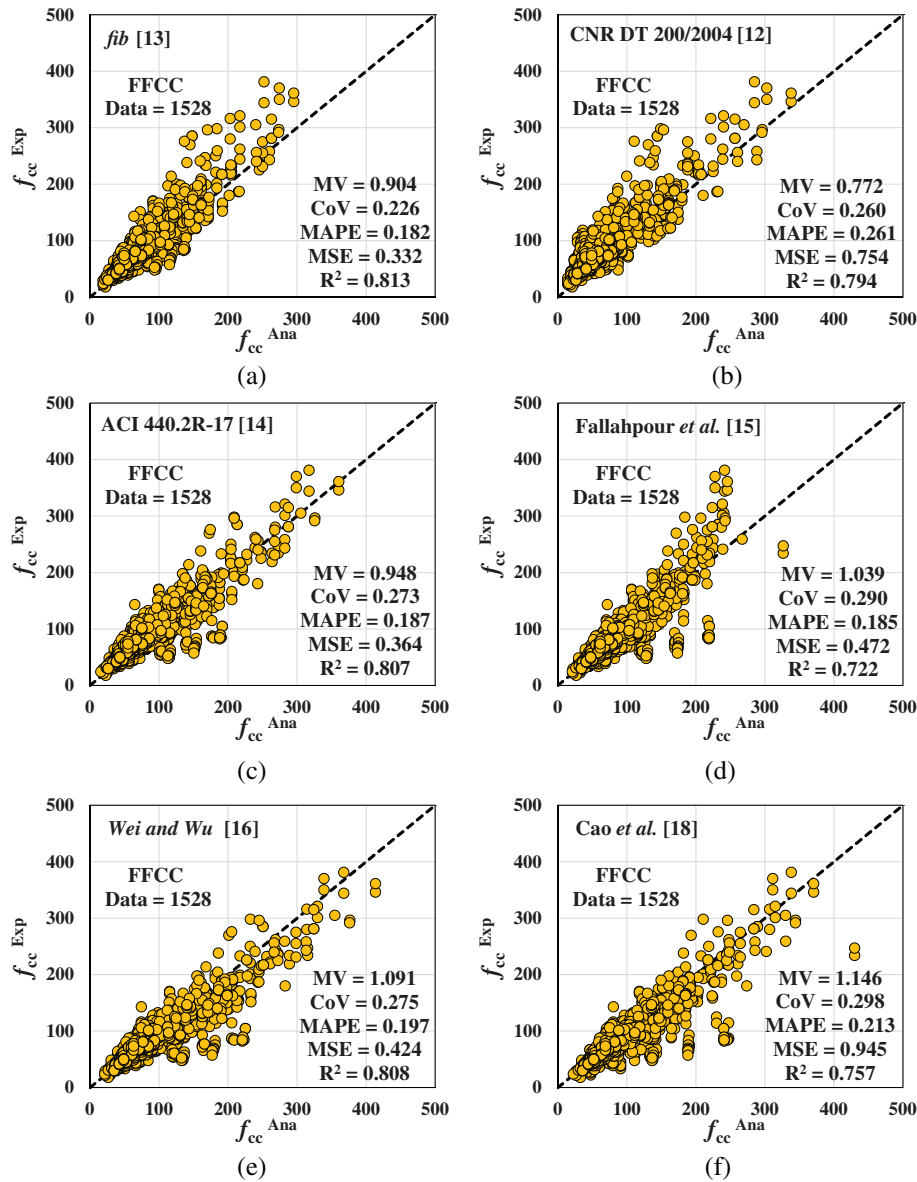


FIGURE 4 Axial compressive strength of fiber-reinforced polymer (FRP) FRP fully confined concrete columns (FFCC): Test versus predicted results. CoV, coefficient of variation; MAPE, mean absolute percentage error; MSE, mean squared error; MV, mean value; R², R-squared

account the stress concentration in square cross-section column with almost sharp edge as:

$$k_r = 2.7 - 10R_b \geq 1 \quad (13)$$

As a result, FRP confinement-induced improvement can be calculated through the proposed model with a unified character for different confining arrangements and cross-section columns (FFCC, FFSC, FPCC, and FPSC).

It should be noted that in a reinforced concrete (RC) column, a certain level of confinement is provided by steel transverse reinforcements. Accordingly, for the real

cases of RC columns wrapped by FRP jacket, the dual internal steel-FRP confinement is imposed to the concrete core. Based on Lin et al.²⁶ and Triantafyllou et al.,²⁷ the peak axial strength of FRP confined RC columns (f_{cc}^{Total}) can be assumed as $f_{cc}^{FRP} + \Delta f_{cc}^{Stirrup}$ where $\Delta f_{cc}^{Stirrup}$ is the steel transverse reinforcements' contribution in the combined steel-FRP confinement and f_{cc}^{FRP} can be calculated by the model proposed in the present study. Therefore, by addressing the effect of steel confinement ($\Delta f_{cc}^{Stirrup}$) based on regression analysis performed on an adequate test database, the proposed model can be extended for the case of FRP confined RC columns, having a unified

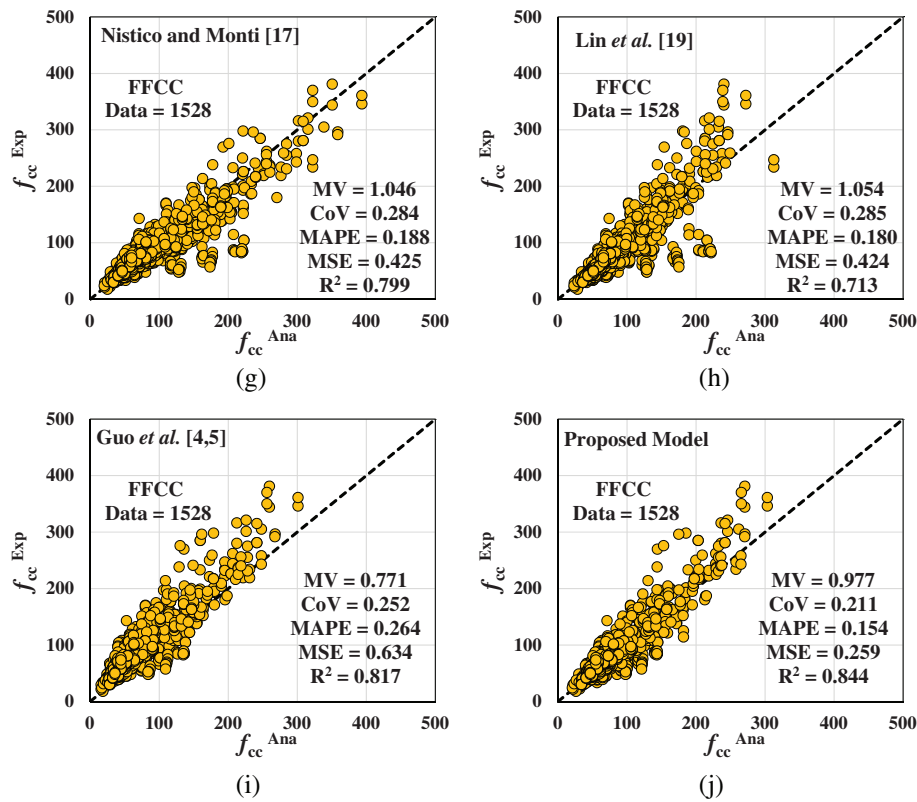


FIGURE 4 (Continued)

TABLE 3 Statistical assessment of existing and proposed models for FFCC

ID	Test data	MV	CoV	MAPE	MSE	R^2
Proposed model	1529	0.977	0.211	0.154	0.259	0.864
Lin et al. ¹⁹		1.054	0.285	0.180	0.424	0.713
<i>fib</i> ¹³		0.904	0.226	0.182	0.332	0.813
Guo et al. ^{4,5}		0.771	0.252	0.264	0.634	0.817
Fallahpour et al. ¹⁵		1.039	0.290	0.185	0.472	0.722
ACI 440.2R-17 ¹⁴		0.948	0.273	0.187	0.364	0.807
Cao et al. ¹⁸		1.146	0.298	0.213	0.945	0.757
Nistico and Monti ¹⁷		1.046	0.284	0.188	0.425	0.799
Wei and Wu ¹⁶		1.091	0.275	0.197	0.424	0.808
CNR DT 200/2004 ¹²		0.772	0.260	0.261	0.754	0.794

Abbreviations: CoV, coefficient of variation; FFCC, FRP fully confined concrete columns; FRP, fiber-reinforced polymer; MAPE, mean absolute percentage error; MSE, mean squared error; MV, mean value; R^2 , R-squared.

character with FRP confined concrete (where $\Delta f_{cc}^{Stirrup} = 0$), which will be the focus of a future research study.

5 | STATISTICAL ASSESSMENTS

In this study, to comprehensively evaluate the reliability and predictive performance of existing models

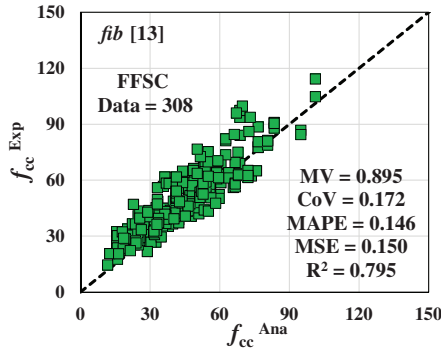
(as presented in Table 2), the experimental tests of the assembled database were simulated with these models, and the obtained results were treated by determining the statistical indicators of mean value (MV in Equation 14), (CoV in Equation 15), mean absolute percentage error (MAPE in Equation 16), mean squared error (MSE in Equation 17), and R-squared (R^2 in Equation 18):

$$MV = \frac{1}{n} \sum_1^n \frac{T_i}{E_i} \tag{14}$$

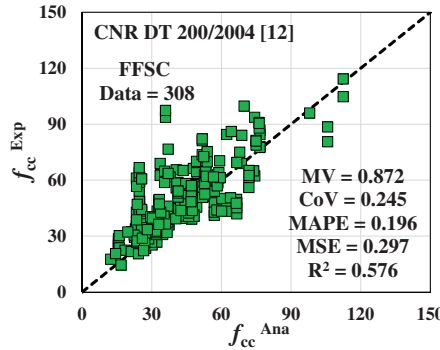
$$MAPE = \frac{1}{n} \sum_1^n \left| 1 - \frac{T_i}{E_i} \right| \tag{16}$$

$$CoV = \frac{SD}{MV} \tag{15}$$

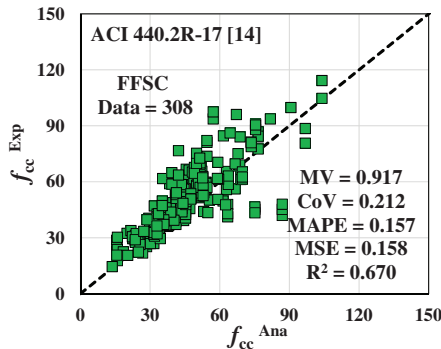
$$MSE = \frac{1}{n} \sum_1^n (T_i - E_i)^2 \tag{17}$$



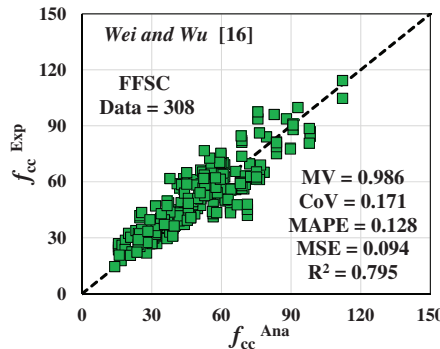
(a)



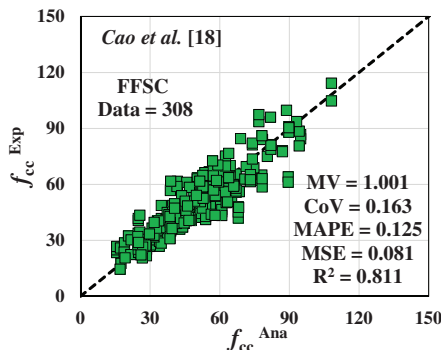
(b)



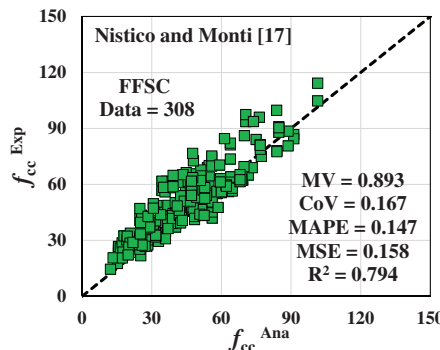
(c)



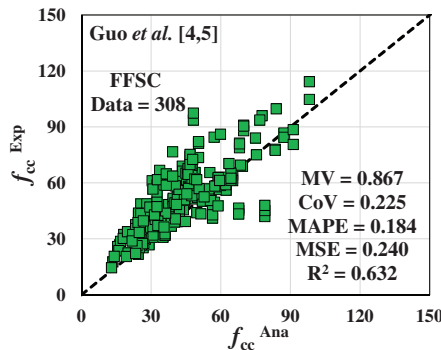
(d)



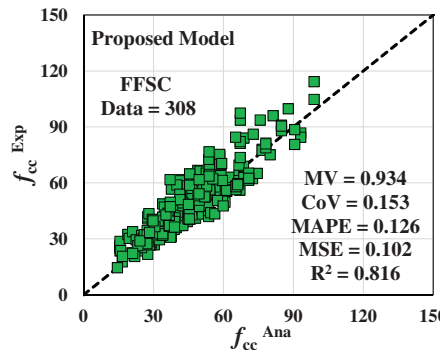
(e)



(f)



(g)



(h)

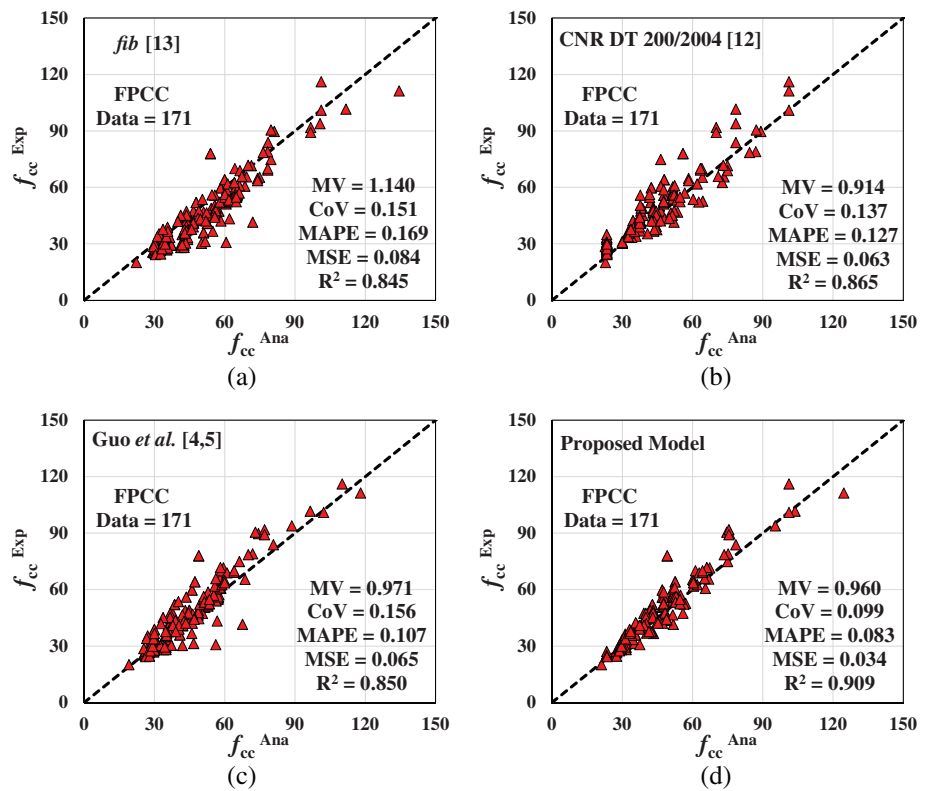
FIGURE 5 Axial compressive strength of fiber-reinforced polymer (FRP) fully confined square cross-section (FFSC): Test versus predicted results. CoV, coefficient of variation; MAPE, mean absolute percentage error; MSE, mean squared error; MV, mean value; R², R-squared

TABLE 4 Statistical assessment of existing and proposed models for FFSC

ID	Test data	MV	CoV	MAPE	MSE	R ²
Proposed Model	308	0.934	0.153	0.126	0.102	0.816
<i>fib</i> ¹³		0.895	0.172	0.146	0.150	0.795
Guo et al. ^{4,5}		0.867	0.225	0.184	0.240	0.632
ACI 440.2R-17 ¹⁴		0.917	0.212	0.157	0.158	0.670
Cao et al. ¹⁸		1.001	0.163	0.125	0.081	0.811
Nistico and Monti ¹⁷		0.893	0.167	0.147	0.158	0.794
Wei and Wu ¹⁶		0.986	0.171	0.128	0.094	0.795
CNR DT 200/2004 ¹²		0.872	0.245	0.196	0.297	0.576

Abbreviations: CoV, coefficient of variation; FFSC, FRP fully confined square cross-section; FRP, fiber-reinforced polymer; MAPE, mean absolute percentage error; MSE, mean squared error; MV, mean value; R², R-squared.

FIGURE 6 Axial compressive strength of fiber-reinforced polymer (FRP) partial confinement system applied to circular column (FPCC): Test versus predicted results. CoV, coefficient of variation; MAPE, mean absolute percentage error; MSE, mean squared error; MV, mean value; R², R-squared



$$R^2 = \left(\frac{\sum_1^n [(T_i - \bar{T})(E_i - \bar{E})]}{\sqrt{\sum_1^n (T_i - \bar{T})^2 (E_i - \bar{E})^2}} \right)^2 \quad (18)$$

where T_i and E_i are f_{cc}/f_{c0} obtained analytically and experimentally, respectively; SD is standard deviation; n is the number of data; \bar{T} and \bar{E} represent the MV of the analytical and experimental predictions, respectively.

Figure 4 and Table 3 compares the predictive performance of existing and proposed model over 1528 experimental data of FFCC. As evidenced, the proposed model provided close and uniform predictions of experimental counterparts based on the main statistical indicators, that

is, CoV = 0.211, MAPE = 0.154, MSE = 0.259, and $R^2 = 0.864$. Even though *fib*⁷ (Figure 4a) and ACI 440.2R-17⁸ (Figure 4c) provided the best performance among the existing models with slight conservative results, the proposed model has better predictive performance in estimating the experimental f_{cc}/f_{c0} .

For the case of fully FRP confined concrete column of square cross-section (FFSC), the predictive performance of proposed and existing models in estimating f_{cc} is compared in Figure 5 and Table 4. As shown, the proposed and Cao et al.¹⁸ models demonstrated the best performance with similar statistical indicator results, and better when compared with the ones of the other models.

ID	Test data	MV	CoV	MAPE	MSE	R ²
Proposed model	171	0.960	0.099	0.083	0.034	0.909
<i>fib</i> ¹³		1.140	0.151	0.169	0.084	0.845
Guo et al. ^{4,5}		0.971	0.156	0.107	0.065	0.850
CNR DT 200/2004 ¹²		0.914	0.137	0.127	0.063	0.865

Abbreviations: CoV, coefficient of variation; FPCC, FRP partial confinement system applied to circular column; FRP, fiber-reinforced polymer; MAPE, mean absolute percentage error; MSE, mean squared error; MV, mean value; R², R-squared.

TABLE 5 Statistical assessment of existing and proposed models for FPCC

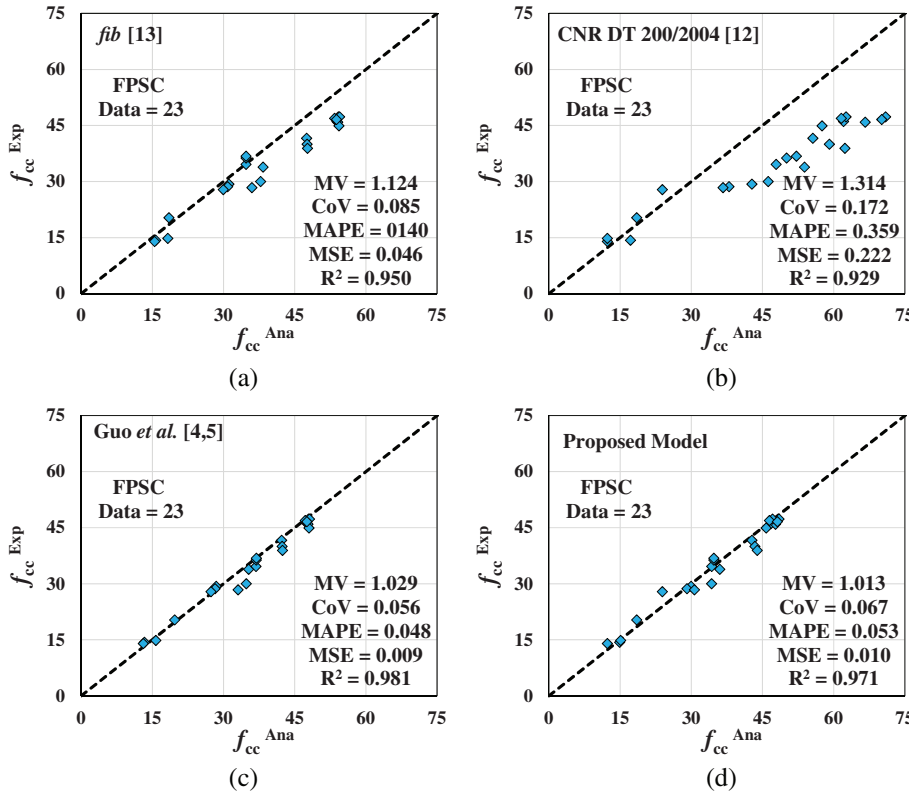


FIGURE 7 Axial compressive strength of fiber-reinforced polymer (FRP) fully confined square cross-section (FPSC): Test versus predicted results. CoV, coefficient of variation; MAPE, mean absolute percentage error; MSE, mean squared error; MV, mean value; R², R-squared

ID	Test data	MV	CoV	MAPE	MSE	R ²
Proposed model	23	1.013	0.067	0.053	0.010	0.971
<i>fib</i> ¹³		1.124	0.085	0.140	0.046	0.950
Guo et al. ^{4,5}		1.029	0.056	0.048	0.009	0.981
CNR DT 200/2004 ¹²		1.314	0.172	0.359	0.222	0.929

Abbreviations: CoV, coefficient of variation; FPSC, FRP partially confined square concrete elements; FRP, fiber-reinforced polymer; MAPE, mean absolute percentage error; MSE, mean squared error; MV, mean value; R², R-squared.

TABLE 6 Statistical assessment of existing and proposed models for FPSC

For the case of partially FRP confined concrete columns of circular cross-section (FPCC), Figure 6 and Table 5 evidence that the proposed model is able to accurately and uniformly predict the experimental f_{cc} . Even though CNR DT 200/2004¹² also provided a good

estimation of experimental counterparts, the proposed model presented the best predictive performance.

For the case of partially FRP confined concrete columns of square cross-section (FPSC), Figure 7 and Table 6 show that the Guo et al.^{4,5} and the proposed

FIGURE 8 Axial compressive strength of fiber-reinforced polymer (FRP) FRP fully confined concrete columns/FRP fully confined square cross-section/FRP partial confinement system applied to circular column/FRP partially confined square concrete elements: Test versus predicted results. CoV, coefficient of variation; FRP fully confined square cross-section; FRP, fiber-reinforced polymer; MAPE, mean absolute percentage error; MSE, mean squared error; MV, mean value; R^2 , R-squared

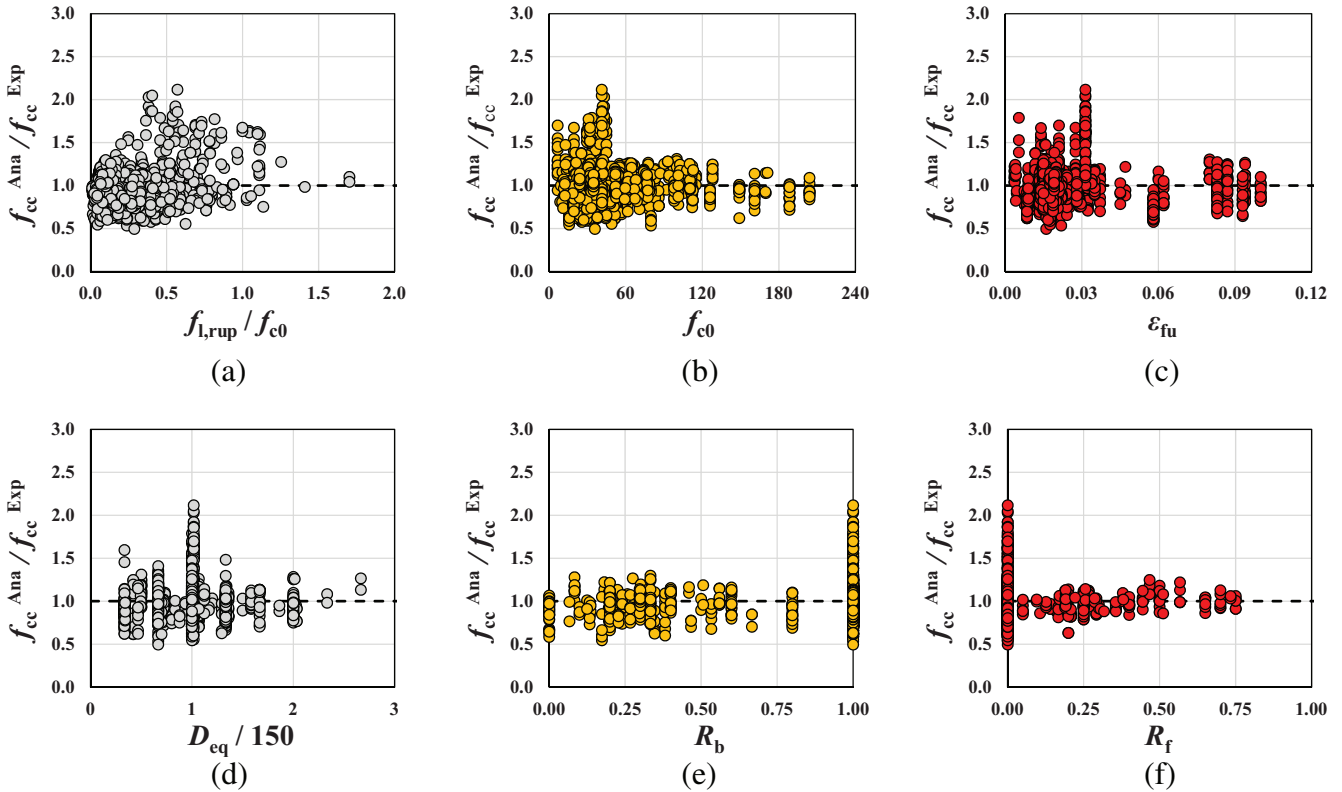
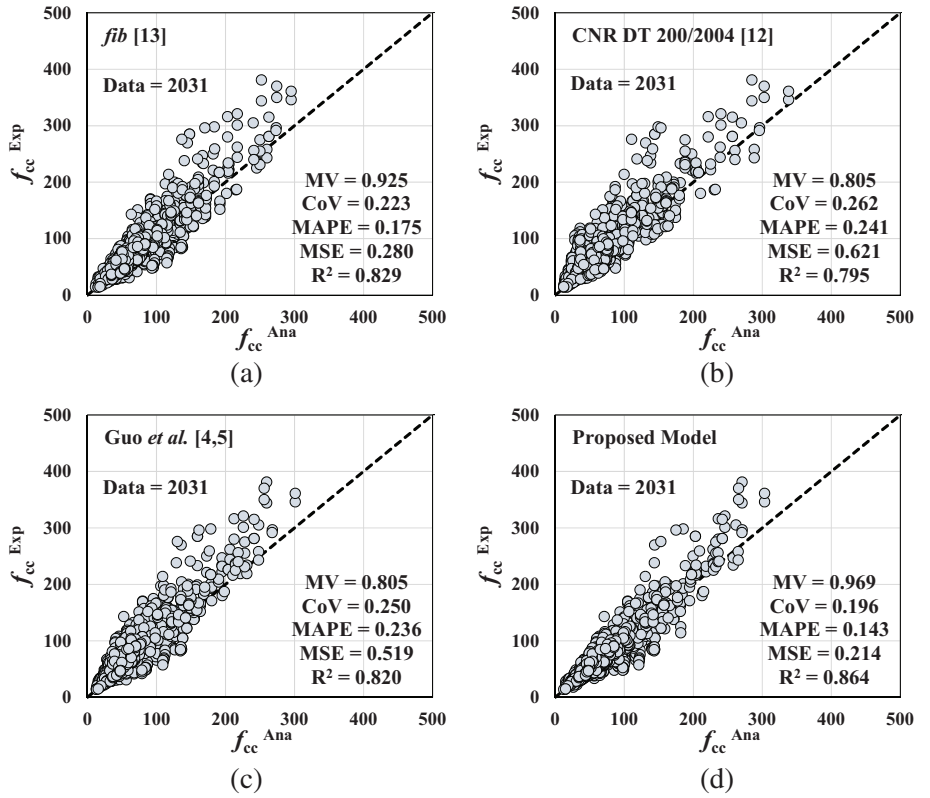


FIGURE 9 Performance of the proposed model with respect to key parameters

models have presented the best performance with almost identical results of statistical indicators, and better than those of *fib*¹³ and CNR DT 200/2004.¹² Nonetheless, the predictive performance of the proposed model was better than Guo et al.^{4,5} in the FFCC, FFSC, and FPCC.

The predictive performance of the proposed model is compared in Figure 8 with the one of the models that have a unified approach for predicting f_{cc} of FFCC, FFSC, FPCC, and FPSC, namely *fib*,¹³ Guo et al.^{4,5} and CNR DT 200/2004.¹² This comparison shows that the proposed model has the best predictive performance in estimating the experimental f_{cc} , confirming its reliability. Among the existing unified models, *fib*¹³ prediction also has a good agreement with experimental counterparts.

For further evaluation of the proposed model, its predictive performance was assessed with respect to key parameters, as demonstrated in Figure 9. As evidenced in Figure 9a, the model has relatively uniform performance for different level of $f_{l,rupt}/f_{c0}$. Figure 9b shows that, even though the effect of f_{c0} was not considered in the establishment of the relation of f_{cc}/f_{c0} and $f_{l,rupt}/f_{c0}$ in Equation (12), there is not any significant correlation between the error ($f_{cc}^{Ana}/f_{cc}^{Exp}$) with respect to f_{c0} . Figure 9c also confirms that there is no obvious variation in model prediction with respect to ε_{fu} . In Figure 9d, the model performance can be also considered uniform for the range of $D_{eq}/150$ of the database. For the case of column of square cross-section (FFSC and FPSC), Figure 9e shows that the model reveals slight conservative predictions with uniform performance for different level of R_b , where a larger scatter was observed in columns of circular cross-section ($R_b = 1$). For the case of partially confined concrete column (FPCC and FPSC), Figure 9f confirms the uniform error distribution with respect to different ranges of R_f even though there is a larger scatter for full confinement cases with $R_f = 0$. In Figure 9e,f, the reliability of the adopted concept of confinement efficiency factor (k_h and k_v presented in Equations 5 and 8, respectively) for the generalization of the cross-section and confining arrangement can also be confirmed.

6 | SUMMARY AND CONCLUSIONS

In this study, a new model with a unified approach for being capable of predicting the peak axial compressive strength (f_{cc}) of concrete columns of different confinement arrangements and of circular or square cross-sections (FFCR, FPCR, FFCC, and FPCC) was developed, and its predictive performance was assessed by using a large database of experimental results, and compared with the one of existing models. For the generalization of

the cross-section and confining arrangement, the concept of confinement efficiency factor with a unified mathematical framework was adopted. For statistical assessment and the calibration of the developed model, a comprehensive database comprising 1528 FFCC, 308 FFSC, 171 FPCC, and 23 FPSC experimental results were collected from the literature. The predictive performance was assessed in terms of MV, CoV, MSE, MAPE, and R^2 . For the data based composed of 2031 experimental results, the developed model has presented the best statistical predictive indicators among the models applicable to FFCR, FPCR, FFCC, and FPCC, namely: MV = 0.969, CoV = 0.196, MAPE = 0.143, MSE = 0.214, $R^2 = 0.864$.

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DATA AVAILABILITY STATEMENT

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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