

1 **Finite element based micro modelling of masonry walls subjected to fire**
2 **exposure: framework validation and structural implications**

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6 **Abstract**

7 This paper presents a 2-D finite element (FE) based micro modelling framework for thermo-
8 mechanical response history analysis of solid brick masonry structures subjected to fire. The 2-D
9 FE framework considers geometric and material nonlinearities, and transient states of strain in
10 conjunction with the temperature-dependent material properties. Material nonlinearity within the
11 2-D FE model is considered by the temperature-dependent total strain rotating crack model. The
12 FE framework is validated against the thermo-mechanical response of a half-scale masonry wall
13 subjected to one-sided fire exposure, and it is observed that the predictions of the FE framework
14 are reasonably accurate. Utilizing the validated FE framework, thermo-mechanical response
15 history characterization is performed on a full-scale masonry wall subjected to one-sided fire
16 exposure. Critical physical phenomena which include thermal bowing, heat diffusion, unit-mortar
17 thermo-mechanical interaction, cracking and stress profiles within the masonry structures are
18 studied intricately. Furthermore, thermo-mechanics within representative volumes enclosing unit
19 as well as mortar and their correlation with the global thermo-mechanical response is studied. Such
20 2-D micro-scale thermo-mechanical computations on masonry walls followed by a detailed
21 discussion on their thermo-mechanics are one of the novel features of the present study. It is

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22 observed that thermal bowing resulted from a complex interaction between thermal dilation and
23 cracking and crushing in the mortar and unit within the masonry structure.

24 **Keywords:** Thermo-mechanical analysis, Masonry, Fire resistance, Nonlinear thermal gradients.

25 **1 Introduction**

26 Ancient and modern infrastructural utilities employ masonry as one of the predominant material
27 for structural and/or non-structural elements attributing to its excellent thermal, mechanical and
28 acoustic properties. The response of such masonry structures has been well studied in the context
29 of static and dynamic loading scenarios [1,2]. However, limited rather scarce understanding is
30 available in the literature in the context of masonry structures subjected to fire exposure [3]. The
31 design of masonry structures subjected to fire is usually done by the fire resistance rating
32 quantification, which is essentially the time required by the structure for attaining the prescribed
33 failure limit state which is usually in terms of strength, integrity and deflection limits [4]. The fire
34 resistance ratings of masonry structures are normally evaluated by a) experimental methods [3], b)
35 codified approaches (e.g. EN 1996-1-2 [4] and ACI 216.1-07 [5]) and c) numerical models (e.g.
36 [6,7]).

37 Experimental methods involve the fire resistance rating quantification by exposing the masonry
38 structure to a given fire scenario. The early experimental investigations on masonry subjected to
39 fire include the full-scale fire tests on clay brick masonry walls conducted at the Experimental
40 building station, Australia [8] to study the phenomenon of fire-induced thermal bowing. Lawrence
41 and Gnanakrishnan [9] conducted a comprehensive experimental investigation on clay brick
42 masonry walls subjected to fire and quantified the effects of slenderness ratio and applied axial
43 load on the overall thermo-mechanical behavior. Shields et al. [10] investigated the thermo-

44 mechanical response of masonry walls subjected to the BS-476 fire exposure. Lavery et al. [11]
45 tested scaled concrete brick masonry walls subjected to various load levels and fire exposures and
46 had explained the phenomena of thermal bowing and reverse thermal bowing. Recently, Nguyen
47 and Meftah [12] experimentally investigated the thermo-mechanical response of hollow clay block
48 masonry walls subjected to fire exposure, and spalling was observed in their experimental
49 investigation. Although such full-scale tests facilitate precise understanding of the thermo-
50 mechanics of the masonry walls, they cannot be performed regularly for the prescriptive and/or
51 performance based design of masonry walls subjected to fire due to the explicit costs and time
52 involved in such tests.

53 Codified approaches essentially involve fire resistance rating quantification of masonry walls
54 from the tabulated data available in the building codes (e.g. EN 1996-1-2 [13], IS-1642 [14] and
55 ACI 216.1-07 [5]) as a function of the wall thickness. However, such an approach is prescriptive
56 in nature and does not account for critical phenomena which may significantly influence the
57 thermo-mechanics of the masonry wall like load level, geometric effects, boundary conditions and
58 realistic fire exposures. These limitations can be alleviated with the aid of experimentally validated
59 numerical models. Very limited numerical investigations have been performed on the numerical
60 simulation of the thermo-mechanical response of the masonry structures subjected to fire. An
61 early numerical model developed in this context includes the 2-D finite element (FE) model
62 developed by Dhansekaran et al. [6]. Their FE model demonstrated thermal bowing in masonry
63 walls and it is essentially a layered shell element which performs time-variant mechanical analysis
64 with thermal gradients and temperature-dependent mechanical properties as input. Nadjai et al.
65 [15] developed a 2-D FE based micro model for nonlinear thermo-mechanical analysis of masonry
66 walls and successfully implemented in MasSET programme [16]. Their 2-D FE model accounts

67 for geometric and material nonlinearities, thermal gradients, temperature-dependent material
68 properties and transient states of strain. Later, they had demonstrated applications pertaining to the
69 behavior of compartmental masonry walls subjected to fire exposure [17] using their MasSET
70 programme. Nguyen and Meftah [18] demonstrated a numerical validation study on a hollow clay
71 block masonry subjected to fire exposure utilizing a nonlinear 3-D FE micro modelling approach
72 in Cast3M. To model the observed spalling in the experiment, their numerical model considered a
73 crushing-detachment-buckling based spalling criteria and was successfully validated against the
74 experimental observations. Recently, Kumar and Srivastava [19] had demonstrated the effect of
75 masonry infill on the in-plane and out of plane response of the fire exposed masonry in-filled
76 reinforced concrete frame utilizing a nonlinear 3-D FE simplified micro model in ANSYS. Their
77 numerical investigation indicated a significant influence of masonry on the overall stability of the
78 masonry in-filled RC frame at elevated temperatures.

79 Aforementioned works pertaining to the numerical modelling of masonry structures provide a
80 perspective on the thermo-mechanical response of masonry walls subjected to fire. However,
81 masonry being a complex material with different thermal and mechanical properties of the
82 constituents, a detailed understanding is needed on the unit level thermo-mechanics and its
83 correlation with the global thermo-mechanical response. Such a discussion is observed to be
84 missing in the present literature and is the prime focus of the present study. This study
85 demonstrates an intricate numerical investigation on masonry walls subjected to fire utilizing a 2-
86 D FE micro model in DIANA-FEA [20]. The unit and mortar are modelled separately within the
87 2-D FE model and it accounts for a) geometric and material nonlinearities, b) nonlinear thermal
88 gradients, c) temperature-dependent mechanical and thermal properties, d) cracking and crushing
89 of materials, and e) transient states of strain.

90 The present paper is organized as follows. Section 2 presents the theoretical aspects of the 2-D FE
91 modelling based simulation framework which include assumptions, thermo-mechanical
92 components of the FE model, and temperature-dependent material models. Next, Section 3
93 presents the experimental validation study pertaining to half-scale masonry wall subjected to fire
94 exposure. Section 4 demonstrates a scenario based thermo-mechanical analysis of full-scale
95 masonry wall subjected to fire exposure. Finally, Section 5 concludes the present study.

96 **2 Simulation framework**

97 This study utilizes a nonlinear 2-D FE micro modelling based framework to evaluate the thermo
98 mechanical behaviour of solid brick masonry walls subjected to fire. The framework is formulated
99 in a plane stress setting assuming a uniform fire exposure and mechanical boundary conditions
100 along the top and bottom surfaces of the wall. In the case of thermal analysis, such an approach is
101 considered ideal as no lateral conduction is expected for such a uniform fire exposure. However,
102 in the case of mechanical analysis such plane stress approach may not be ideal in case of walls
103 with complete or partial lateral restraint (in the direction perpendicular to the 2D simulation plane).
104 Moreover, the unit-joint thermo-mechanical interactions along the lateral direction are ignored.
105 Such a 2-D framework with above mentioned plane stress idealization facilitates computationally
106 efficient thermo-mechanical analysis of masonry walls subjected to fire. However, in scenarios
107 involving a deviation of the aforementioned assumption, 3-D FE modelling should be preferred.
108 Furthermore, the developed framework in its present form is not applicable for the thermo-
109 mechanical analysis of hollow-brick masonry walls.

110 It is to be noted that FE based computational modelling of masonry is usually done utilizing micro
111 and macro based modelling strategies, respectively [2]. Within the micro modelling, which is the

112 main focus of the present study, three approaches are possible, namely: a) detailed micro
113 modelling, b) continuum micro modelling, and c) simplified micro modelling (Figure 1). In the
114 case of detailed micro modelling, the unit, mortar and the unit-mortar interface are modelled
115 separately. Continuum micro modelling is a simplified version of detailed micro modelling
116 strategy, with bonded interfaces. In the case of simplified micro modelling strategy, unit and
117 mortar are modelled together as a composite unit with interface elements at the half thickness of
118 the mortar. These approaches have their own merits and de-merits and have been a matter of
119 discussion among various researchers (e.g. Lourenço [2] and Mohyeddin [21]). In the context of
120 thermo-mechanical modelling of masonry exposed to fire, detailed micro modelling strategy
121 facilitates precise modelling of physical phenomena and is capable of considering localized failure
122 modes (cracking, crushing and various modes of fracture at the unit-mortar interface).

123 However, at elevated temperatures, the temperature-dependent mechanical behavior of the unit-
124 mortar interface is still not established due to the lack of comprehensive experimental research,
125 specifically targeted to the temperature-dependency of the nonlinear interface behavior.

126 This limitation can be partly alleviated by extending the temperature-dependency in mechanical
127 properties of cement mortar to the unit-mortar interface. However, detailed model calibration
128 studies are required to account for the lack of experimental data pertaining to the temperature-
129 dependent coupled tension-shear failure mode in cement mortar [22] . Furthermore, convergence
130 issues are expected due to the complex temperature-dependent interface nonlinearity. In view of
131 such complex limitations, the present study models unit and mortar separately in a combined
132 geometric and material nonlinearity setting using the continuum micro modelling strategy.
133 Although such approach does not account for temperature-dependent interface behaviour, it

134 accounts for the localized failures expected in the mortar joints as well as units and such approach
135 has been successfully implemented in the past as well (e.g. [15,18]). Utilizing the aforementioned
136 modelling strategy in the considered framework, the thermo-mechanical response histories of
137 masonry walls are demonstrated in the present study.

138 Figure 2 shows the 2-D FE model which performs thermo-mechanical analysis with various
139 thermal and mechanical boundary conditions. The thermo-mechanical analysis is performed
140 utilizing a staggered one-way coupling scheme. In such a scheme, the thermal analysis is
141 performed first on a fixed geometry followed by time-variant mechanical analysis at constant
142 temperatures corresponding to various time steps [23]. Such a scheme is computationally efficient
143 unlike the theoretically precise monolithic schemes [23] which might lead to a large system of
144 equations with asymmetry and eventually makes the analysis computationally very intensive. In
145 the context of the present simulation framework, the need for a fully coupled strategy has been
146 demonstrated to be of relatively small importance, hence the staggered analysis strategy is chosen.
147 The theoretical aspects of the individual thermal and mechanical FE models are discussed in
148 Sections 2.1 and 2.2 respectively.

149 **2.1 Thermal FE model**

150 For a 2-D body as shown in Figure 2, the heat transfer is governed by conduction, convection and
151 radiation. Within the 2-D solid body enclosed by Ω , heat transfer is governed by thermal
152 conduction, whereas the heat transfer from the heating source to the exposed boundaries is
153 governed by convection and radiation. The governing equation to model the heat transfer is
154 deduced from the law of energy balance and is given by

155
$$(\rho c)_T \frac{\partial T}{\partial t} = \nabla \cdot (\gamma_T \nabla T), \quad (1)$$

156 where $(\rho c)_T$ represents temperature-dependent specific heat capacity, T represents temperature, γ_T
 157 represents temperature-dependent thermal conductivity tensor. It is to be noted that the external
 158 fire temperature is applied either as Dirichlet or Neuman boundary condition (convection and
 159 radiation). The governing equations for the convection and radiation on the boundary Γ_N are given
 160 by

161
$$\begin{aligned} (\gamma \nabla T) \cdot \mathbf{n} &= -h_c (T - T_f), \\ (\gamma \nabla T) \cdot \mathbf{n} &= -h_r \left[(T + 273.15)^4 - (T_f + 273.15)^4 \right], \end{aligned} \quad (1)$$

162 where T_f represents the fire temperature, h_c represents the convective heat transfer coefficient, h_r
 163 ($h_r = \chi \zeta \xi$) represents the radiative heat transfer coefficient, χ represents the form factor, ζ
 164 represents the emissivity, and ξ represents the Stefan-Boltzmann constant ($5.678 \times 10^{-8} \text{W/m}^2 \text{K}^4$).
 165 Ritz-Galerkin FE discretization is applied to Equation (1) utilizing the eight-node quad element
 166 and two-node line element as shown in Figure 2. The eight-node quad element work on the solid
 167 body enclosed by Ω , and with four integration points in a full integration setting. Whereas the two-
 168 node line element work on the boundary convection and radiation at the Γ_N , and with two
 169 integration points in a full integration setting. Upon discretization, a system of equations is obtained
 170 as [24]

171
$$\mathbf{M} \dot{\mathbf{T}}(t) + \mathbf{K} \mathbf{T}(t) = \boldsymbol{\psi}(t), \quad (2)$$

172 where \mathbf{M} represents the heat capacity matrix, \mathbf{K} represents the conductivity matrix and $\boldsymbol{\psi}(t)$
 173 represents the heat load vector. These systems of equations are highly nonlinear in nature due to

174 temperature-dependent material properties and boundary conditions and are solved iteratively
175 using the Newton-Raphson method until the L_2 norm of temperature reaches the prescribed value
176 of tolerance.

177 **2.2 Mechanical FE model**

178 For the 2-D FE model as shown in Figure 2, the time-variant mechanical analysis component is
179 executed in a one-way coupling scheme, with the temperature history of the previously executed
180 thermal analysis as an input. For the 2-D body enclosed by Ω , the Galerkin FE discretization is
181 applied using 8-node quad element with four integration points in a full integration setting.
182 Subsequently, the incremental equilibrium equations are obtained as

$$183 \quad \mathbf{K}\Delta\mathbf{d} = \Delta\mathbf{F}_m + \Delta\mathbf{F}_{th}, \quad (3)$$

184 where \mathbf{K} represents the temperature-dependent element stiffness matrix derived in a total
185 Lagrangian based formulation, $\Delta\mathbf{d}$ represents the element displacement vector, $\Delta\mathbf{F}_m$ represents
186 the incremental force vector pertaining to mechanical loading, and $\Delta\mathbf{F}_{th}$ represents the incremental
187 force vector pertaining to thermal effects. The incremental system of equations shown in Equation
188 (4) are derived from the principle of virtual work [24] in conjunction with temperature-dependent
189 constitutive relation ($\boldsymbol{\sigma} = \mathbf{D}_T(\boldsymbol{\varepsilon} - \boldsymbol{\varepsilon}_T)$). Wherein, $\boldsymbol{\sigma}$ represents the second Piola-Kirchhoff tensor,
190 \mathbf{D}_T represents the temperature-dependent constitutive matrix, $\boldsymbol{\varepsilon}$ represents the total Green-
191 Lagrange strain, $\boldsymbol{\varepsilon}_T$ represents the total thermal strain. A detailed description of the strain
192 components and the constitutive matrix will be discussed subsequently. Equation (4) is highly
193 nonlinear in nature and is solved iteratively. In the present study, the Newton-Raphson based

194 nonlinear solution strategy is followed with a prescribed tolerance value of 0.001 on the L₂ norms
195 of energy.

196 2.3 Material models

197 This section illustrates the temperature-dependent material models used within the 2-D FE
198 modelling based simulation framework. In the context of thermal analysis, the temperature-
199 dependency in $(\rho c)_T$ and γ_T in the context of thermo-mechanical modelling of masonry walls will
200 be discussed in the respective numerical simulation sections, respectively. The total Green-
201 Lagrange strain ($\boldsymbol{\varepsilon}$) discussed in Section 2.2 is decomposed as

$$\begin{aligned} \boldsymbol{\varepsilon} &= \boldsymbol{\varepsilon}_m + \boldsymbol{\varepsilon}_T, \\ \boldsymbol{\varepsilon}_T &= \boldsymbol{\varepsilon}_{th} + \boldsymbol{\varepsilon}_{tc}, \end{aligned} \quad (4)$$

203 where $\boldsymbol{\varepsilon}_m$, $\boldsymbol{\varepsilon}_{th}$ and $\boldsymbol{\varepsilon}_{tc}$ represent mechanical strain, total thermal strain, thermal strain and transient
204 creep strains, respectively. A perspective on the additive decomposition of concrete strains under
205 transient thermal conditions can be seen in [25,26]. The thermal strain is computed as

$$\boldsymbol{\varepsilon}_{th} = \alpha_T \Delta T, \quad (5)$$

207 where α_T is the temperature-dependent coefficient of thermal expansion. The transient creep
208 strain in the present FE model, the transient creep strain is modelled using the empirical
209 relationship proposed by Anderberg and Thelanderson [27] as

$$\Delta \boldsymbol{\varepsilon}_{tc} = \tau \left(\frac{\sigma}{f_{c,20}} \right) \Delta \boldsymbol{\varepsilon}_{th}, \quad (6)$$

211 where σ represents stress at a given time, $f_{c,20}$ represents the compressive strength of concrete at
212 20 °C and τ is constant which ranges between 1.8 and 2.5. Further, details of the transient creep
213 strain in the context of the present study will be explained in the respective numerical simulation
214 sections. It is to be noted that the standard creep is not considered in combination with the transient
215 creep in the simulation framework, as the considered time scales are very small eventually resulting
216 negligible contribution from the standard creep [27]. The mechanical strain is governed by the
217 temperature-dependent constitutive relation ($\boldsymbol{\sigma} = \mathbf{D}_T (\boldsymbol{\varepsilon} - \boldsymbol{\varepsilon}_T)$) and is computed using the total
218 strain rotating crack model. Consideration of rotating crack model instead of a fixed crack model
219 has been a matter of discussion among various researchers after it was first introduced by Cope et
220 al. [28]. In the fixed crack model, the material axes of symmetry are fixed throughout the analysis
221 and it may result in inaccurate model predictions in scenarios involving a change in the principal
222 directions during the course of loading [29]. This limitation has been circumvented with the aid of
223 rotating crack model, where the misalignment between the principal directions and principal axes
224 of symmetry is adjusted by co-rotating the principal axes of symmetry. In a total strain rotating
225 crack model based constitutive framework, the temperature-dependent constitutive matrix (\mathbf{D}_T) is
226 computed from the 1-D temperature-dependent inelastic constitutive relations (Figure 3) in the
227 tensile and compressive regimes, respectively. The background theory for such numerical
228 implementation can be seen in [28,30] and not repeated here for the sake of brevity.

229 In case of tension regime, the 1-D inelastic constitutive relation is elastic with linear softening as
230 shown in Figure 3 and is characterized by the temperature-dependent tensile strength ($f_{t,T}$) and
231 fracture energy corresponding to mode-1 ($G_{f1,T}$). The temperature dependency of above
232 mentioned parameters in the context of the present study will be discussed in the respective

233 numerical simulation studies. In the case of compression regime, a parabolic curve with linear
234 softening as in EN1992-1-2 [31] is considered for 1-D inelastic constitutive relation and is
235 characterized by temperature-dependent compressive strength ($f_{c,T}$), strain at peak compressive
236 strength ($\varepsilon_{cp,T}$) and ultimate compressive strain ($\varepsilon_{cu,T}$).

237 **3 Simulation of the experiment of half-scale masonry subjected to fire**

238

239 The accuracy of the 2-D FE based simulation framework is established by validating the
240 experimental investigation of Lavery et al. [11]. Their experimental study essentially involves a
241 half-scale masonry wall (b=430 mm; h=1330 mm; t=50 mm) subjected to one-sided fire exposure
242 as shown in Figure 4. The half-scale wall is built with concrete bricks (100×32×50 mm) with 20
243 MPa compressive strength, bedded on 1:3 cement-sand mortar mix (5 mm thick) pertaining to
244 ordinary Portland cement. The wall is rested on a firm steel base and an axial load of 50 kN, which
245 is 50% of the design ultimate load is applied on the wall through the steel plate, which is restrained
246 against lateral translation as shown in Figure 4. The temperatures were measured at the central
247 vertical third positions (h/3 and 2h/3) of the wall at various depths (0, t/6, t/2, 5t/6 and t) along the
248 cross-section, whereas the lateral deflections were measured at the mid-span, top and bottom,
249 respectively. Utilizing the simulation framework, thermo-mechanical analysis is performed with
250 the mesh-size shown in Figure 4. The chosen mesh size is based on mesh convergence studies.

251 To quantify the effect of temperature-dependent material nonlinearity, the analysis is also
252 performed in a thermo-elastic setting with temperature-dependent thermal and mechanical
253 properties. It is to be noted that in the present simulation framework, geometric effects which
254 include large deformations, large rotations and large strains are modelled by the total Lagrangian

255 formulation (TLF) [32]. To quantify the effect of large strains, additional thermo-mechanical
256 analysis is performed without considering the geometric effects. The wall is fixed at the base and
257 restrained against lateral translation at the top as shown in Figure 4. The mechanical load is applied
258 with the aid of a steel plate, and such loading is simulated by modelling steel plate separately with
259 a line interface between steel plate and wall ($K_n=56\text{ kN/m}^3$; $K_t=5.6\text{ kN/m}^3$) and the tensile strength
260 of the interface is taken as zero. Such values are chosen from the elastic material properties of the
261 steel plate in conjunction with the mesh characteristics.

262 **3.1 Material properties**

263 The material properties utilized for validating the aforementioned experimental investigation in
264 the context of present 2-D FE framework is presented herein. A summary of these properties at
265 room temperature ($T=20\text{ }^\circ\text{C}$) is shown in Table 1.

266 The temperature-dependency in specific heat capacity and thermal conductivities of concrete unit
267 and cement mortar are taken from the EN1992-1-2 [31] and are shown in Figure 5. It should be
268 noted that there is no specific mention of aforementioned thermal properties in the experimental
269 investigation of Lavery et al [11]. The properties from EN1992-1-2 [31] have been chosen as they
270 explicitly account for the latent heat effects pertaining to the inherent moisture within the masonry
271 wall. A moisture content of 3% by weight is assumed in the present validation study. As will be
272 shown subsequently, the chosen thermal properties resulted in reasonably accurate thermal
273 histories. The temperature-dependent thermal expansion coefficient for concrete unit as well as
274 cement mortar are taken from the EN1992-1-2 [31] corresponding to that of calcareous aggregates.

275 The coefficient τ pertaining to the transient creep strain is taken as 2.0 for both concrete unit and
276 cement mortar, and such value has been ascertained from the parametric studies. The required

277 material properties pertaining to the rotating crack constitutive framework discussed in Section
278 2.3, at $T=20$ °C are taken from the studies of Laverty et al. [11,15]. It is to be noted that the
279 temperature-dependency in aforementioned mechanical properties is taken from EN1992-1-2 [31].
280 This is attributed to their predominate applications by the fire engineering community as well as
281 the lack of comprehensive experimental investigation pertaining to the constituent materials of the
282 half-scale test. The temperature-dependency in compressive and tensile strengths of concrete unit
283 and cement mortar is shown in Figure 6. The temperature-dependency in $\varepsilon_{cp,T}$ and $\varepsilon_{cu,T}$ of concrete
284 unit and cement mortar is shown in Figure 7. Further, the temperature-dependent mode-1 fracture
285 energy of concrete unit and cement mortar are computed from the empirical relation provided by
286 FIB model code [33], which is written as

$$287 \quad G_{f1} = 73f_c^{0.18}. \quad (7)$$

288 **3.2 Results and discussion**

289 A comparison of thermal and mechanical (out of plane deflection) response histories of the half-
290 scale masonry wall is shown in Figure 8, for both the elastic and inelastic cases. The temperature
291 histories at the designated locations shown in Figure 4 are in good agreement with their
292 experimental counter parts with maximum error of 3.14%. The mechanical deflection history is in
293 reasonably good agreement with the experimentally observed values with failure time
294 corresponding to 23 min (numerical failure), whereas the experimentally observed failure time is
295 28 min. The elastic mechanical response history is imprecise in comparison to the experimentally
296 observed values, although it demonstrates thermal bowing. The effect of geometric nonlinearity
297 on the thermo-mechanical response history is shown in Figure 9. It is observed that the mechanical
298 (out of plane deflection) response history is inaccurate with reference to the experimentally

299 observed values, when the geometric effects are not considered. Also, reverse thermal bowing is
300 observed unlike in the experiment as well as the geometric nonlinear simulation, which is due to
301 the temperature-dependent material degradation and damage. Furthermore, the results indicate the
302 importance of consideration of geometric effects in the purview of present simulation framework.
303 The mechanical response history of the central line of the wall is shown in Figure 10. This response
304 indicates thermal-bowing of the wall and its amplification at the verge of failure. The response of
305 masonry wall subjected to fire is governed by the combined effects of nonlinear thermal gradients,
306 geometric effects, applied load, boundary conditions and temperature-dependent material
307 degradation.

308 A discussion on these phenomena in the context of the masonry wall under consideration and their
309 contribution to the mechanical response history is explained herein. Figure 11 and Figure 12, show
310 the thermo-mechanical response of the wall under consideration at $t=5$ min and $t=23$ min,
311 respectively.

312 It should be mentioned that tensile stresses are considered positive, whereas the compressive stress
313 are considered negative and such notation is followed over the entire paper. Firstly, the results at
314 $t=5$ min indicate temperature-diffusion across the wall which eventually resulted in nonlinear
315 thermal gradients across the wall thickness and overall thermal expansion of the wall. It is to be
316 noted that, in the process of attaining a quasi-static equilibrium, such nonlinear thermal gradients
317 result in additional stresses in masonry wall which are compressive in the heated zone and tensile
318 in the adjacent non-heated zone. However, the nature of these stress states are further influenced
319 by the applied mechanical load and boundary conditions.

320 For instance, the presence of a fixed base and a hinged boundary condition at the top of the wall
321 under consideration resulted in an additional temperature-induced restraint stresses which are
322 compressive in the heated zone and tensile in the non-heated zone. The influence of these restraint
323 stresses are evident near the fixed base (see σ_{yy} , Figure 11).

324 Such a combined stress state resulting from thermal dilation and mechanical boundary conditions
325 resulted in a thermal-bowing profile as shown in Figure 10. Further, no cracking was observed in
326 the wall upto $t=5$ min. However, after further fire exposure, the thermal diffusion accelerates and
327 the stress states are predominantly influenced by temperature-dependent material degradation in
328 conjunction with cracking and crushing. This can be seen in the thermo-mechanical response at
329 $t=23$ min (Figure 12), where one can see the predominant tensile zone that induced cracking at the
330 base. Further, such localized cracking significantly influenced the overall mechanical response of
331 the structure and this is explained herein with the aid of thermo-mechanical response histories of
332 representative volume units (RVU) taken at heights of 0.66m (Figure 13) and 0 m (Figure 14)
333 from the base, respectively.

334 Moreover, the stress (σ_{yy}) histories at the designated locations , labelled as M_A , M_B and M_C (see
335 Figure 13) in the aforementioned RVUs are shown in Figure 15. During initial stages of fire
336 exposure, in the case of RVU-1, the observed stress states (see Figure 13, $t=5$ min) are governed
337 by the thermal gradients as well as the fire induced restraint stress due to the fixed base. This
338 resulted in an increase in the compressive stress in the heated zone (Figure 15, RVU-1, M_A) and
339 reduction in the compressive stress in the adjacent non-heated zone (Figure 15, RVU-1, M_B).
340 Whereas in the case of RVU-2, an increase in in the compressive stress in the heated zone (Figure

341 15, RVU-2, M_A) and reduction in the compressive stress in the non-heated zone (Figure 15, RVU-
342 2, M_B & M_C) are observed.

343 However, the increase is higher compared to RVU-1 and is attributed to the predominance of fire
344 induced restraint stresses at the base. After further fire exposure, a shift of the compressive zone
345 is observed in case of RVU-1 towards the unexposed face (See Figure 13, σ_{yy}).

346 This is characterized by a reduction in compressive stresses in the heated zone (Figure 15, RVU-
347 1, M_A) and an increase in compressive stress in the adjacent non-heated zone (Figure 15, RVU-1,
348 M_B). This is attributed to the temperature-dependent material degradation in the heated zone in
349 conjunction with the nonlinear thermal gradients arising due to further heat diffusion.

350 Whereas in the case of RVU-2, cracking is initiated at the base and an increase in the cracking
351 zone is observed with further fire exposure (Figure 14, Normal cracking stress). This is
352 characterized by tensile stress histories in the non-heated zone (Figure 15, RVU-2, M_B & M_C).
353 Furthermore, in the case of RVU-1, an increase in compressive stress is observed in the non-heated
354 zone (Figure 15, RVU-1, M_C). This is attributed to excessive cracking and crushing at the base in
355 RVU-2 (Figure 14, Normal cracking stress) and such cracking and crushing releases the tensile
356 stresses originating from the base. At $t=23$ min, further cracking is observed in RVU-2 and
357 resulted in the partial release of the rotational restraint at the base. This is characterized by a change
358 in the stress-states in RVU-1 (Figure 13) and further resulted in the onset of large out of plane
359 displacements (see Figure 10) and eventually the failure of the masonry wall. However, in the
360 experimental investigation by Laverty et al. [11,15], on the half-scale masonry wall under
361 consideration, detailed observations pertaining to the aforementioned cracking induced collapse

362 were not taken. Lavery et al. [11,15] reported that the fire exposed side of the wall could not be
363 seen due limitations specifically targeted to their scaled fire test.

364 **3.3 Parametric studies**

365 To quantify the effect of assumed parameters, as well as to demonstrate the accuracy of the
366 developed FE framework, parametric studies are performed on the half-scale masonry wall. Figure
367 16a shows the parametric study on transient creep strain, where the coefficient τ (See section 2.3)
368 is varied between 1.8 to 2.4. The results indicate that the increase in τ results in increase in the
369 failure temperature and is due to the reduction in the total thermal strain. Figure 16b shows
370 parametric study on the effect of initial tensile strength of mortar ($f_{t,20}$), where the tensile strength
371 is varied between 0.8 to 1.2 MPa.

372 The results indicate slight increase in the failure temperature with increase in the tensile strength
373 of mortar, with almost similar thermo-mechanical response history. Also, parametric study is
374 performed on the temperature-dependency of the tensile strength of mortar and unit. The
375 temperature-dependency as in Thelandersson [34] is compared to that of the EN1992-1-2 [31].
376 The thermo-mechanical response histories are observed to be similar in both the cases, with
377 slightly higher failure temperature in the case of EN1992-1-2 [31].

378 **4 Full-scale masonry wall subjected to ISO-834 fire exposure**

379 Taking advantage of the previously discussed simulation framework, it was decided to study a
380 different type of masonry wall. This full-scale wall is made of solid clay bricks and the
381 arrangement of the bricks differs from the previous one. This full-scale masonry wall shown in
382 Figure 18 is subjected to ISO-834 fire curve, which is also shown in the figure. The wall is loaded

383 axially and is fixed at the base, and is free to translate and rotate at the top. The design axial load
384 capacity of the wall is quantified in accordance with the EN1996-1-1 [35] and its corresponding
385 fire resistance rating for 50% of the design axial load on the wall is observed to be 240 min from
386 the EN1996-1-2. Thermo-mechanical analysis is performed using the 2-D FE based simulation
387 framework with the mesh-size shown in Figure 18. As discussed in the case of half-scale masonry
388 wall, thermo-elastic analysis is also performed with temperature-dependent thermal and
389 mechanical properties. Axial load corresponding to 50% of the load-carrying capacity of wall is
390 applied in the form of pressure at the top of the wall, which is 0.853 MPa.

391 **4.1 Material properties**

392 The material properties utilized for the full-scale masonry wall are presented herein. A summary
393 of these properties at room temperature ($T=20\text{ }^{\circ}\text{C}$) is shown in Table 2. In the case of cement
394 mortar, the temperature-dependent thermal and mechanical properties are taken from Section 3.1.
395 In the case of clay unit, the temperature-dependency in specific heat capacity and thermal
396 conductivities of clay unit is taken from the EN1996-1-2 [13] and is shown in Figure 19.

397 Due to the lack of availability of comprehensive studies on the nature of transient creep strain in
398 clay unit [36], the transient creep component is ignored in the present numerical simulation. The
399 temperature-dependent thermal expansion coefficient for the clay unit is taken from the EN1996-
400 1-2 [13]. The temperature-dependent $f_{c,T}$, $\varepsilon_{cp,T}$ and $\varepsilon_{cu,T}$ are taken from EN1996-1-2 [13]. It is to
401 be noted that the temperature-dependency of above mentioned parameters is shown up to $750\text{ }^{\circ}\text{C}$
402 in EN1996-1-2 [13], and for higher temperatures beyond $750\text{ }^{\circ}\text{C}$, linear extrapolation is followed
403 in the present study (see Figure 20 and Figure 21). In case of $f_{t,T}$, due to the lack of data (both

404 experimental and code provisions), the temperature-dependency in $f_{t,T}$ is assumed to be the same
405 as that of $f_{c,T}$.

406 The mode-1 fracture energy corresponding to room temperature is taken from the work of
407 Lourenço et al. [37] and to it, the same temperature-dependency as in $f_{t,T}$ is applied, assuming a
408 constant ductility index.

409 **4.2 Results and discussion**

410 The deformed configuration of the central line (scaling 10x) of the wall is shown in Figure 22a.
411 The deformation history of top of the wall is shown in Figure 22b, for both the elastic and inelastic
412 cases, respectively. Significant thermal bowing is observed and the rate of increase of thermal
413 bowing is more predominant in the initial one hour. This is attributed to the nature of the ISO-834
414 fire curve coupled with lower thermal conductivities of unit and mortar, which eventually resulted
415 in higher thermal increments during the initial one hour of fire exposure. However, no reverse
416 thermal bowing was observed for the masonry wall. It is to be noted that the deformation histories
417 are similar for both the elastic and inelastic cases, respectively unlike the half scale wall.

418 However, in the elastic case, higher thermal bowing is observed in comparison to the inelastic case
419 during the later stages of fire exposure. This is attributed to additional eccentricity due to the fire
420 induced material cracking. Figure 23 and Figure 24 show the overall thermo-mechanical response
421 of the masonry walls at $t=5$ min and $t=240$ min, respectively. Upon exposure to fire, highly
422 nonlinear thermal gradients are induced on to the structure and eventually, the presence of such
423 nonlinear thermal gradients coupled with the mechanical load will result in the overall thermal
424 expansion of the wall. However, as discussed in the case of half-scale masonry wall subjected to

425 fire, the thermal expansion in the heated zone results in tension in the adjacent non-heated zone of
426 the structure and eventually culminate into compressive stress in the heated zone. This
427 phenomenon can be seen in Figure 23 ($t=5$ min) where the σ_{yy} at the exposed face is in
428 compression, whereas the adjacent core to the exposed face is in tension. However, the stress states
429 in the masonry wall are transient in nature due to nonlinear thermal gradients coupled with
430 temperature-dependent material degradation and eventually severe cracking is observed in the wall
431 at $t=240$ min (Figure 24, Normal cracking stress). The further explanation pertaining to such
432 thermo-mechanics in the context of the present wall is provided with the aid of RVU-1 (Figure
433 25) and RVU-2 (Figure 26) taken at 1 m and 0 m heights from the base, respectively. The stress
434 (σ_{yy}) histories at the designated locations, M_A , M_B and M_C (see Figure 23) in the considered RVUs
435 are shown in Figure 27. In the case of RVU-1, the heated zone is under compression followed by
436 tension in the adjacent cold zone (Figure 25, σ_{yy} at $t=5$ min). However, as time progresses, the
437 aforementioned compression-tension zone transits over the wall thickness (Figure 25, σ_{yy} at $t= 60$
438 & 120 min) due to which, cracking is observed in the mortar (Figure 25, Normal cracking stress)
439 which is relatively weaker compared to the brick units. These effects can be seen in the stress
440 history plots as well (Figure 27, RVU-1, M_A & M_B). Moreover, after further fire exposure, a
441 reduction in the compressive stress is observed in the heated zone, whereas reduction in tensile
442 stress is observed in the adjacent non-heated zone (Figure 27, RVU-1, M_A & M_B).

443 This is mainly due to two thermo-mechanical phenomena. Firstly, change in the nature of nonlinear
444 thermal gradients attributed to the cross-sectional heat diffusion. Secondly, due to the
445 predominance of the material degradation over thermal dilation in the development of the thermal
446 stresses. It should be mentioned that the discontinuity in stress profiles are observed at the brick-
447 mortar interface (Figure 25, σ_{yy}), unlike the earlier half-scale wall due to the additional stresses

448 generated due to the differential thermal expansion between the brick and mortar. For instance, for
449 the chosen material properties, thermal increment of 1000 °C attributes to a differential thermal
450 strain of 0.00066 which is significant enough to cause additional stresses.

451 Moreover, such stresses have resulted in vertical cracking (see Figure 25, normal cracking stress
452 at $t=120$ and 240 min) in brick and mortar in the hot and cold zones, respectively. In the case of
453 RVU-2 as well, above mentioned thermo-mechanical phenomena were observed with
454 quantitatively similar stress (Figure 27, RVU-2) histories to that of RVU-1, with additional stresses
455 and cracking zones attributing to the base restraint effects. Lastly, for the full-scale masonry wall
456 under consideration, no failure was observed from the numerical simulation, both in terms of
457 strength as well as the insulation failure criteria for the 240 min one-sided fire exposure.

458 **5 Conclusions**

459 A 2-D FE based simulation framework has been developed for thermo-mechanical analysis of
460 solid brick masonry walls. The developed framework modelled unit and mortar separately, and
461 accounted for geometric and material nonlinearities, transient states of strain and temperature-
462 dependent material properties. The developed framework was considered validated as the thermo-
463 mechanical predictions of half-scale masonry wall subjected to fire and the predictions were
464 reasonably accurate, as compared to the experimental results. Utilizing the developed framework,
465 thermo-mechanical analysis was performed on a full-scale masonry wall subjected to one-sided
466 fire exposure.

467 Critical phenomena which included heat diffusion, nonlinear thermal gradients, unit-mortar
468 thermo-mechanical interaction, cracking and stress profiles within the masonry structure were

469 studied in detail in the above mentioned numerical investigations. Also, thermo-mechanics within
470 a representative volume of unit and mortar at various locations were studied. Such unit level
471 thermo-mechanics studies within the present numerical investigation have indicated the following
472 insights. In both the walls, influence of boundary conditions was observed on the stress histories
473 in the representative volume units. In case of the half-scale wall, extensive cracking and crushing
474 in the masonry wall, especially near the base had resulted in the change in the kinematic
475 equilibrium of the global structure and eventually culminated to the failure of the structure. In case
476 of the full-scale clay brick masonry wall, progressive cracking was observed over time. However,
477 no failure was observed in the numerical simulation for the given fire exposure, which was taken
478 from the fire resistance ratings tabulated in EN1996-1-2. Moreover, the differential thermal
479 expansion between the constituent materials of the masonry walls has resulted in additional
480 stresses at the unit-mortar joint, and eventually resulted in vertical cracking profiles near the joints.
481 Lastly, the developed 2-D FE simulation framework and subsequent detailed thermo-mechanical
482 response history characterization demonstrated in the present study facilitates wide range of
483 numerical applications pertaining to masonry structures. They include a) performance based
484 structural fire design, b) sensitivity analysis, c) post-fire residual capacity assessment studies, and
485 d) development of simplified empirical models.

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585 **Tables**

586

587 **Table 1: Physical properties of half-scale masonry wall subjected to fire ($T= 20\text{ }^{\circ}\text{C}$).**

Physical property	Value
Geometry	See Figure 4
Applied load (kN)	50
Concrete unit:	
Compressive strength (MPa)	20
Tensile strength (MPa)	2
Poisson's ratio	0.17
$\varepsilon_{cp,20}$	0.0023
$\varepsilon_{cu,20}$	0.005
Thermal expansion coefficient ($/^{\circ}\text{C}$)	6×10^{-6} (Calcareous aggregates)
Heat capacity (kJ/m ³ K)	2100
Thermal Conductivity (W/mK)	1.36
Mortar joint:	
Compressive strength (MPa)	10
Tensile strength (MPa)	1
Poisson's ratio	0.2
$\varepsilon_{cp,20}$	0.004
$\varepsilon_{cu,20}$	0.009
Thermal expansion coefficient ($/^{\circ}\text{C}$)	6×10^{-6} (Calcareous aggregates)
Heat capacity (kJ/m ³ K)	2100
Thermal Conductivity (W/mK)	1.36

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Table 2: Physical properties of full-scale masonry wall subjected to fire.

Physical property	Value
Geometry	See Figure 18
Applied load (MPa)	0.8538
Clay unit:	
Compressive strength (MPa)	30
Tensile strength (MPa)	3
Poisson's ratio	0.17
$\epsilon_{cp,20}$	0.00175
$\epsilon_{cu,20}$	0.0019
Thermal expansion coefficient (/°C)	5.33×10^{-6} (Clay units)
Heat capacity (kJ/m ³ K)	676
Thermal Conductivity (W/mK)	0.42
mode-1 fracture energy (N/m)	55
Mortar joint:	
Compressive strength (MPa)	10
Tensile strength (MPa)	1
Poisson's ratio	0.2
$\epsilon_{cp,20}$	0.0025
$\epsilon_{cu,20}$	0.02
Thermal expansion coefficient (/°C)	6×10^{-6} (Calcareous aggregates)
Heat capacity (kJ/m ³ K)	2100
Thermal Conductivity (W/mK)	1.36

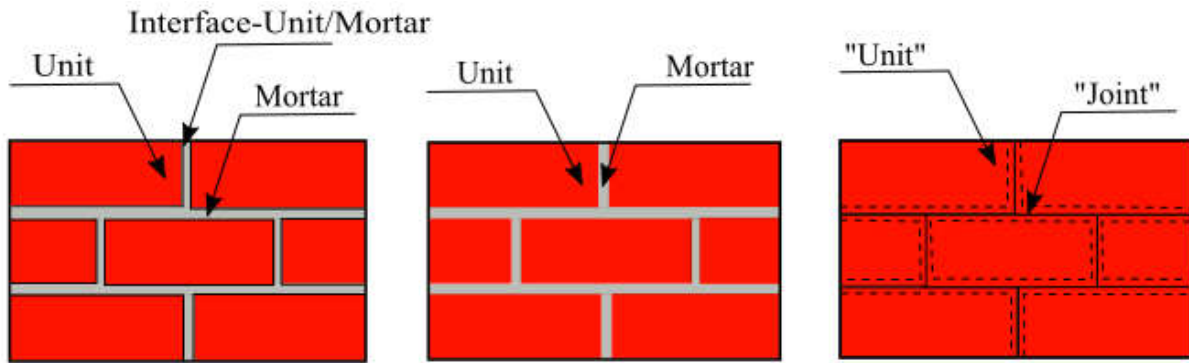
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594 **Figures**

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596



597 a) Detailed Micro model

b) Continuum Micro model

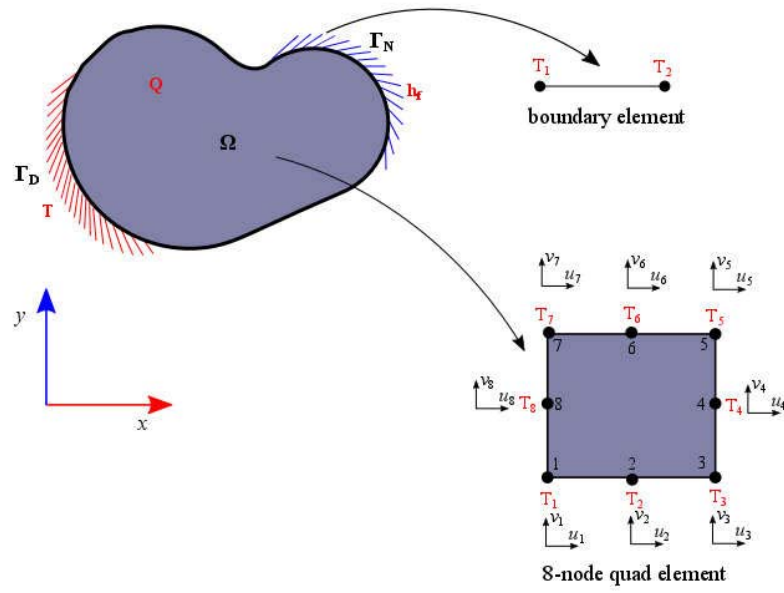
c) Simplified Micro model

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Figure 1: Micro modelling strategies in masonry [2].

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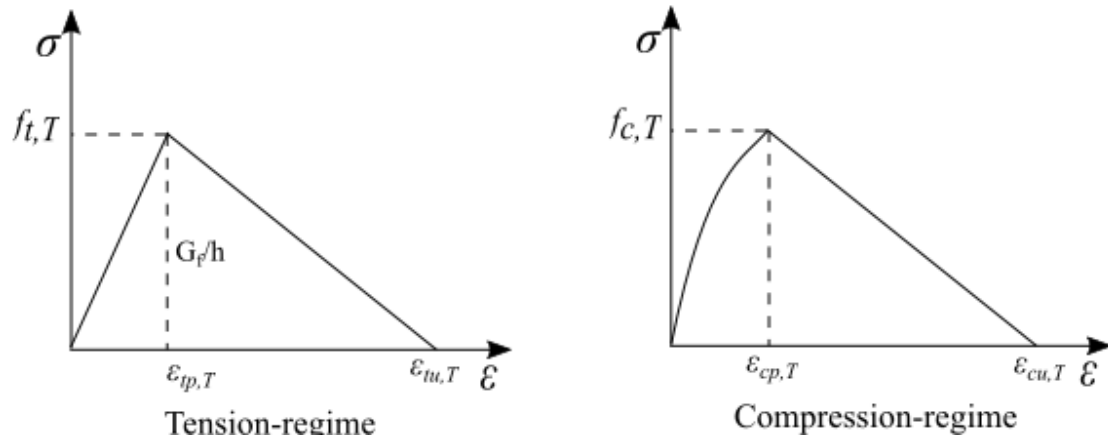
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Figure 2: 2-D Thermo-mechanical modelling and discretization strategy.

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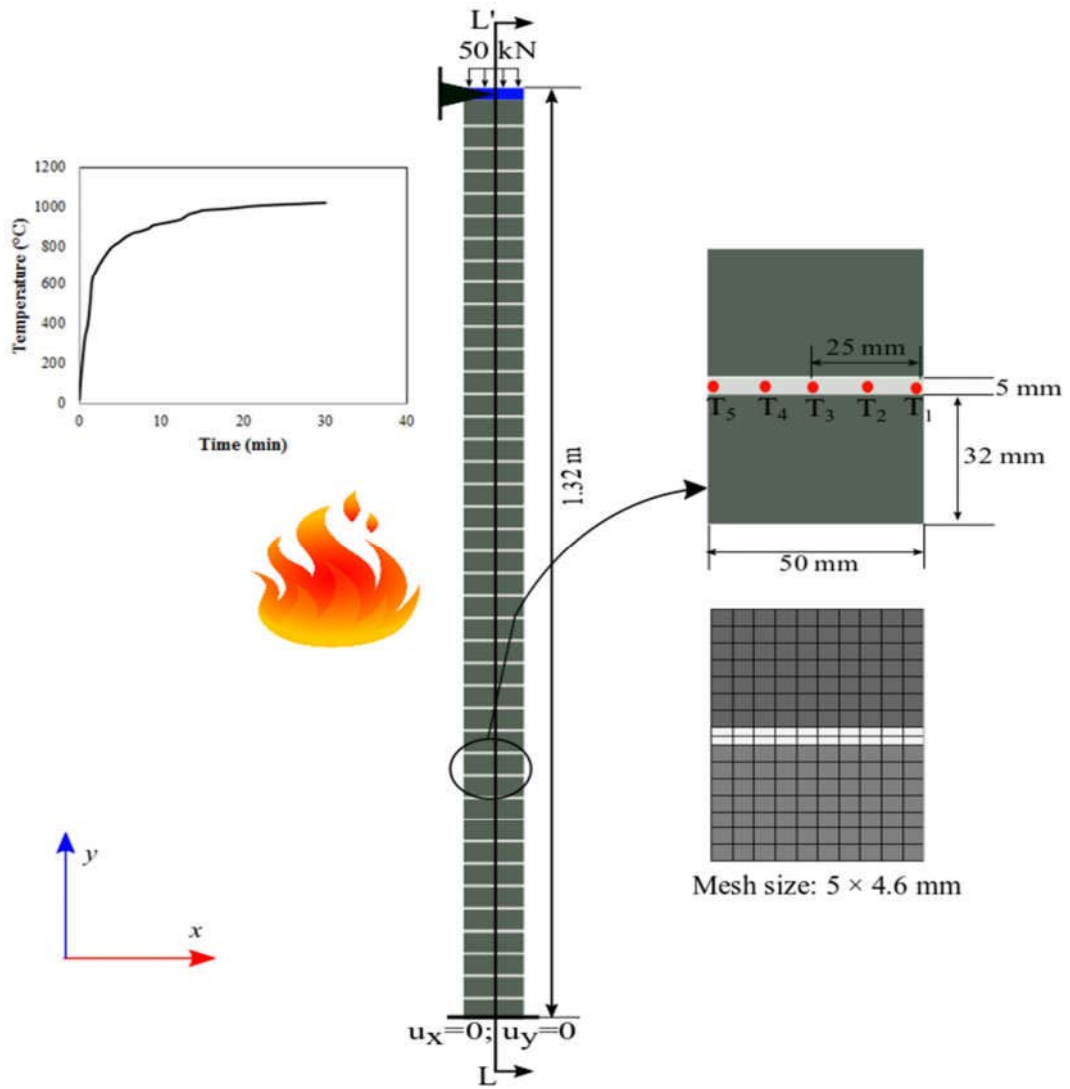
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Figure 3: 1-D tension and compression constitutive behavior used in the total-strain rotating crack model.

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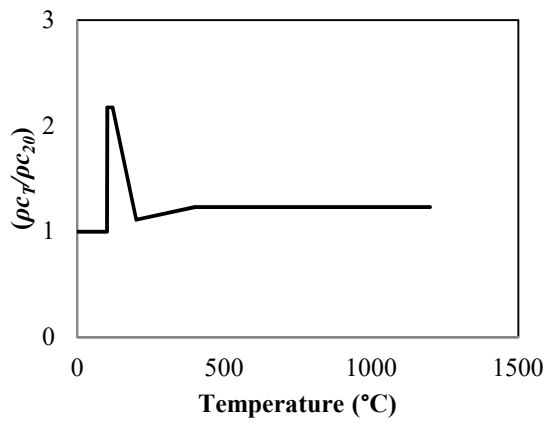
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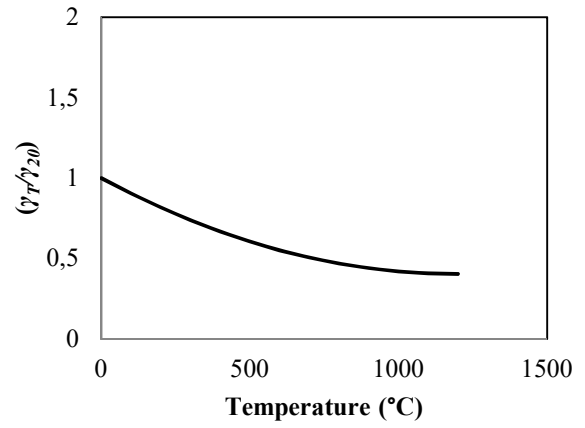
Figure 4: Half-scaled masonry wall subjected to fire.

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a) Specific-heat capacity

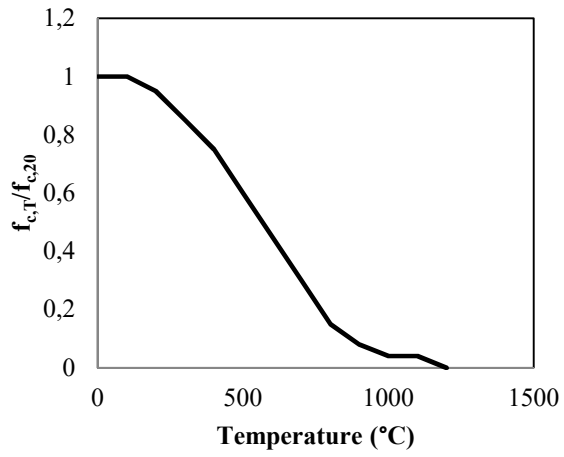


b) Thermal-conductivity

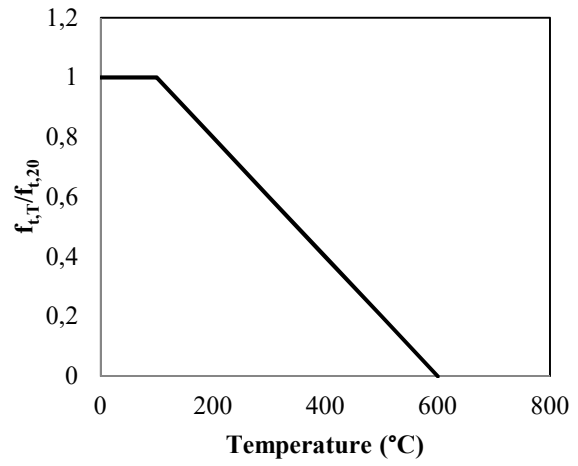
614 **Figure 5: Temperature-dependent thermal properties of concrete unit and cement mortar.**

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a) Compressive strength ($f_{c,T}$)

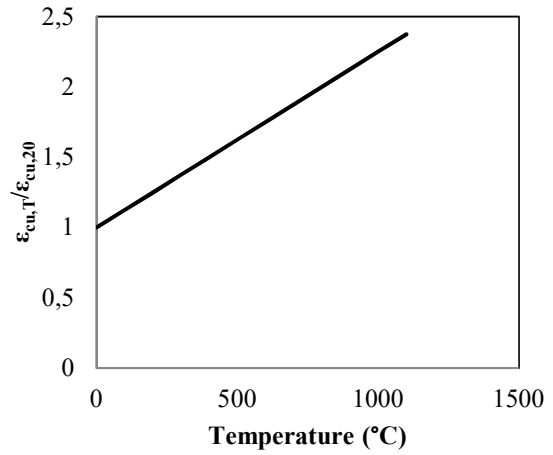
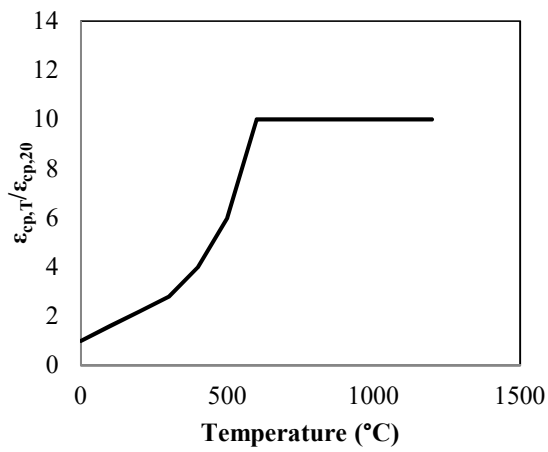


b) Tensile strength ($f_{t,T}$)

617 Figure 6: Temperature-dependent compressive and tensile strengths of concrete unit and cement
618 mortar.

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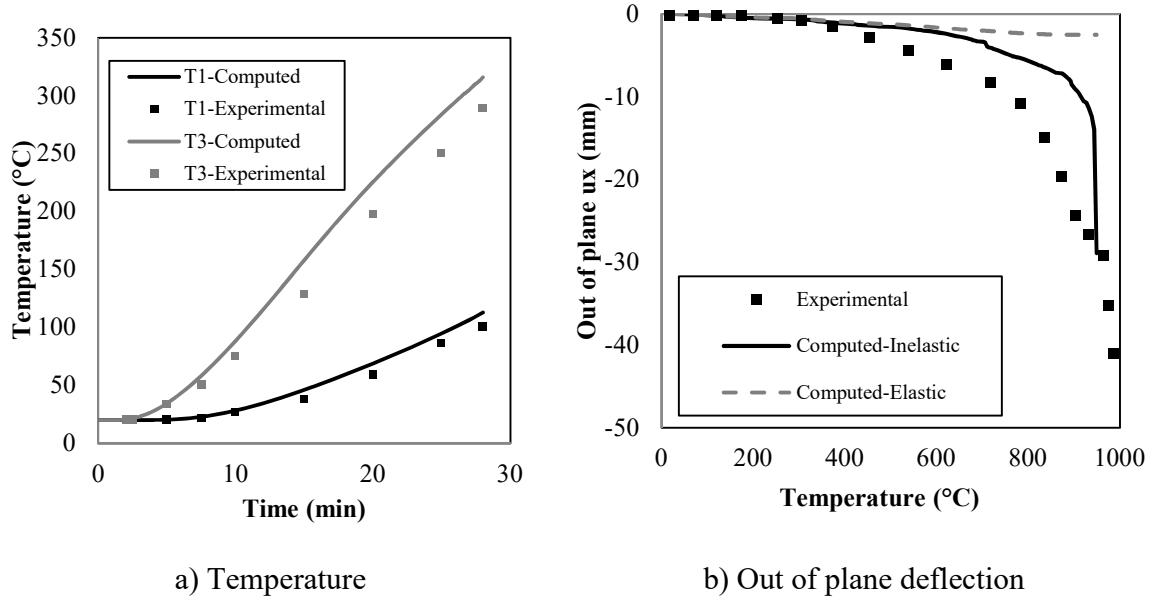
a) Strain at peak compressive strength ($\epsilon_{cp,T}$)

b) Ultimate compressive strain ($\epsilon_{cu,T}$)

621 **Figure 7: Temperature-dependent $\epsilon_{cp,T}$ and $\epsilon_{cu,T}$ of concrete unit and cement mortar.**

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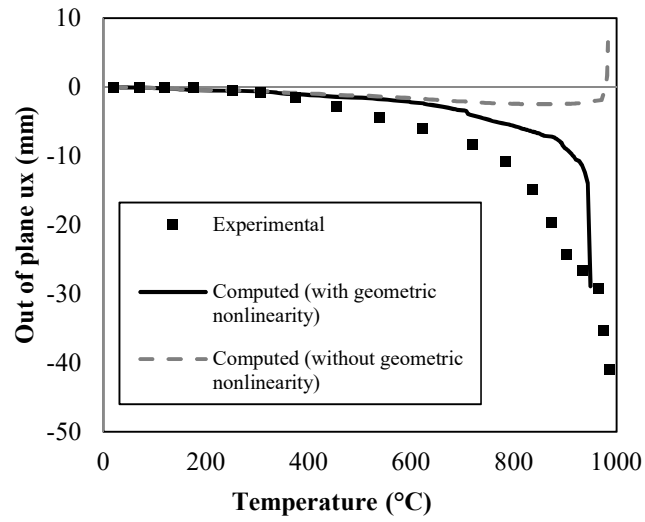


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Figure 8: Comparison of experimental and computed response.

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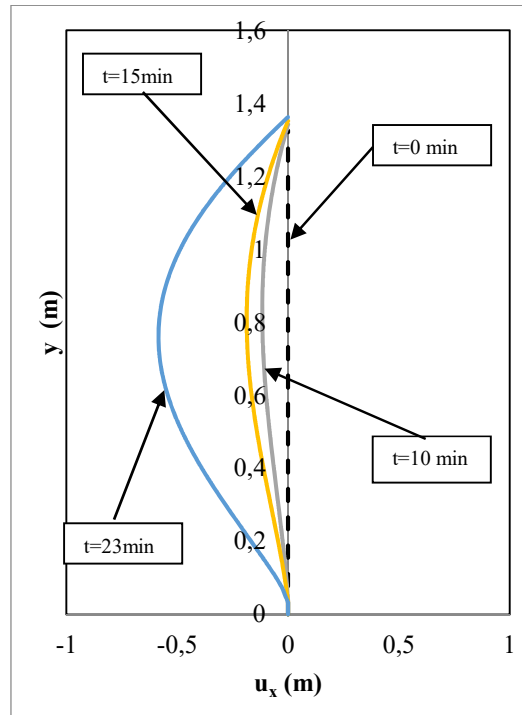


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628 **Figure 9: Effect of geometric nonlinearity on the thermo-mechanical response of the half-**
629 **scale wall.**

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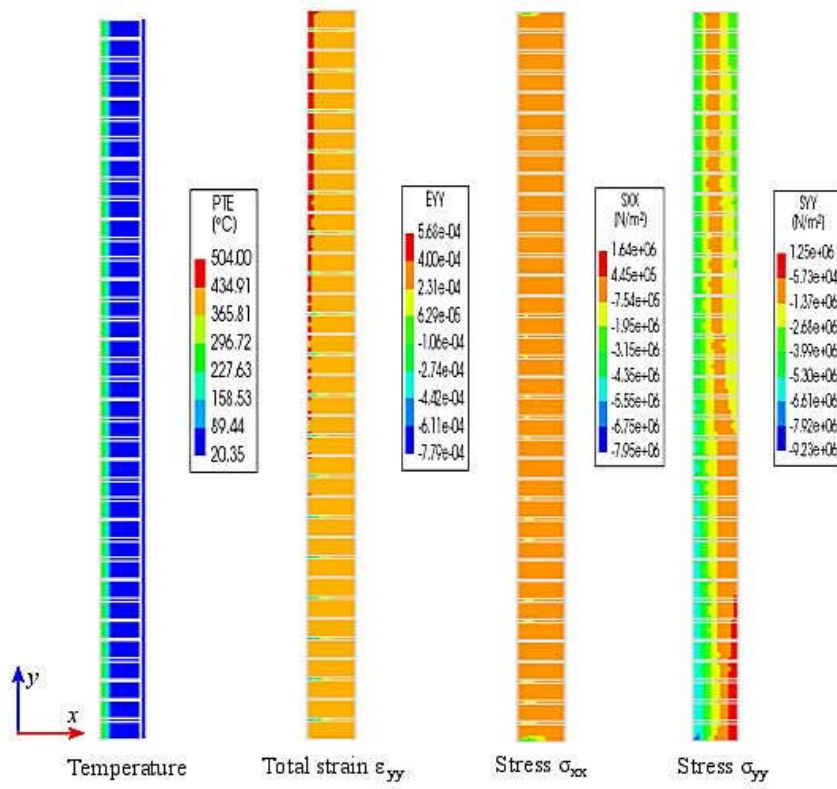


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633 **Figure 10: Deformed configuration of the central line of the half-scale wall (Scaling 30x)**

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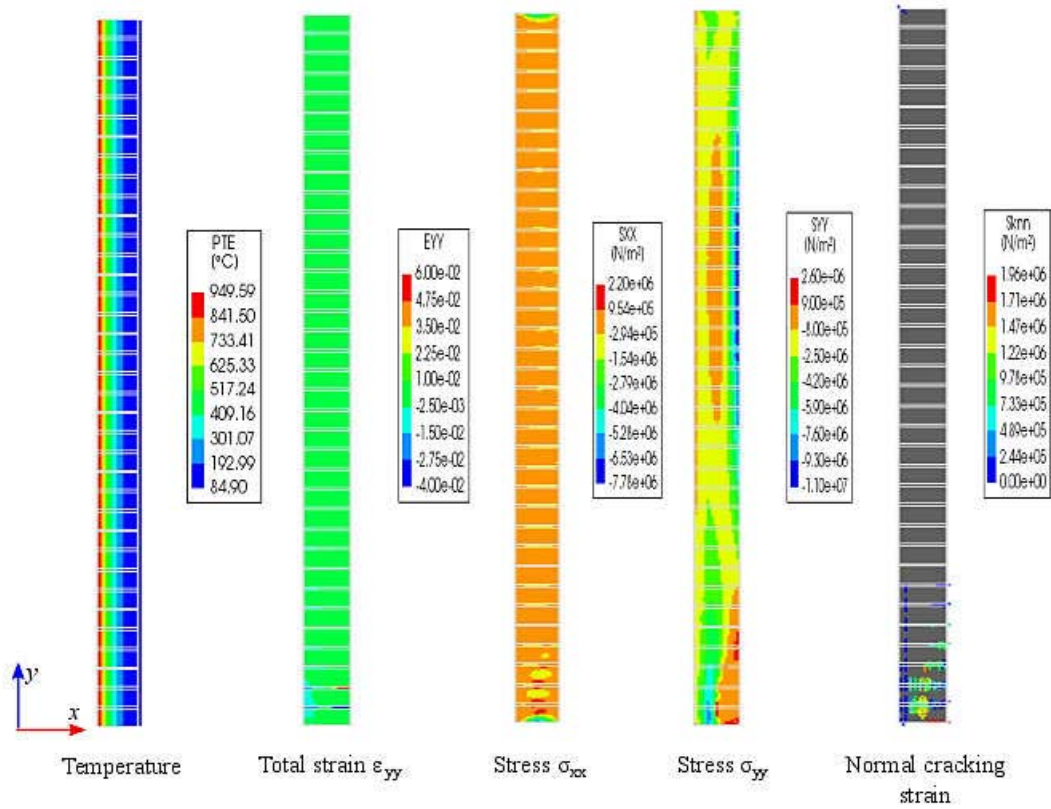
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Figure 11: Thermo-mechanical response of half-scale masonry wall at $t=5$ min.

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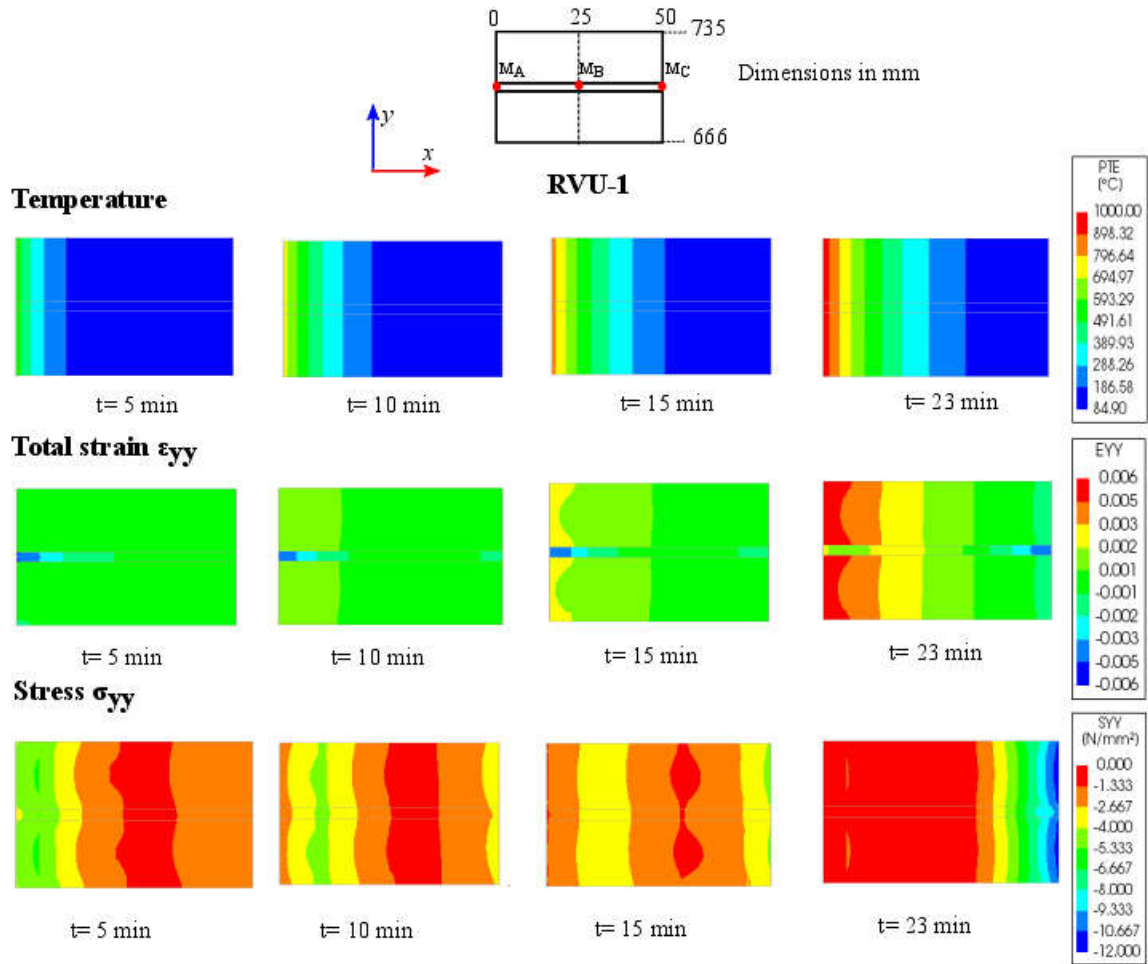
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Figure 12: Thermo-mechanical response of half-scale masonry wall at t=23 min.

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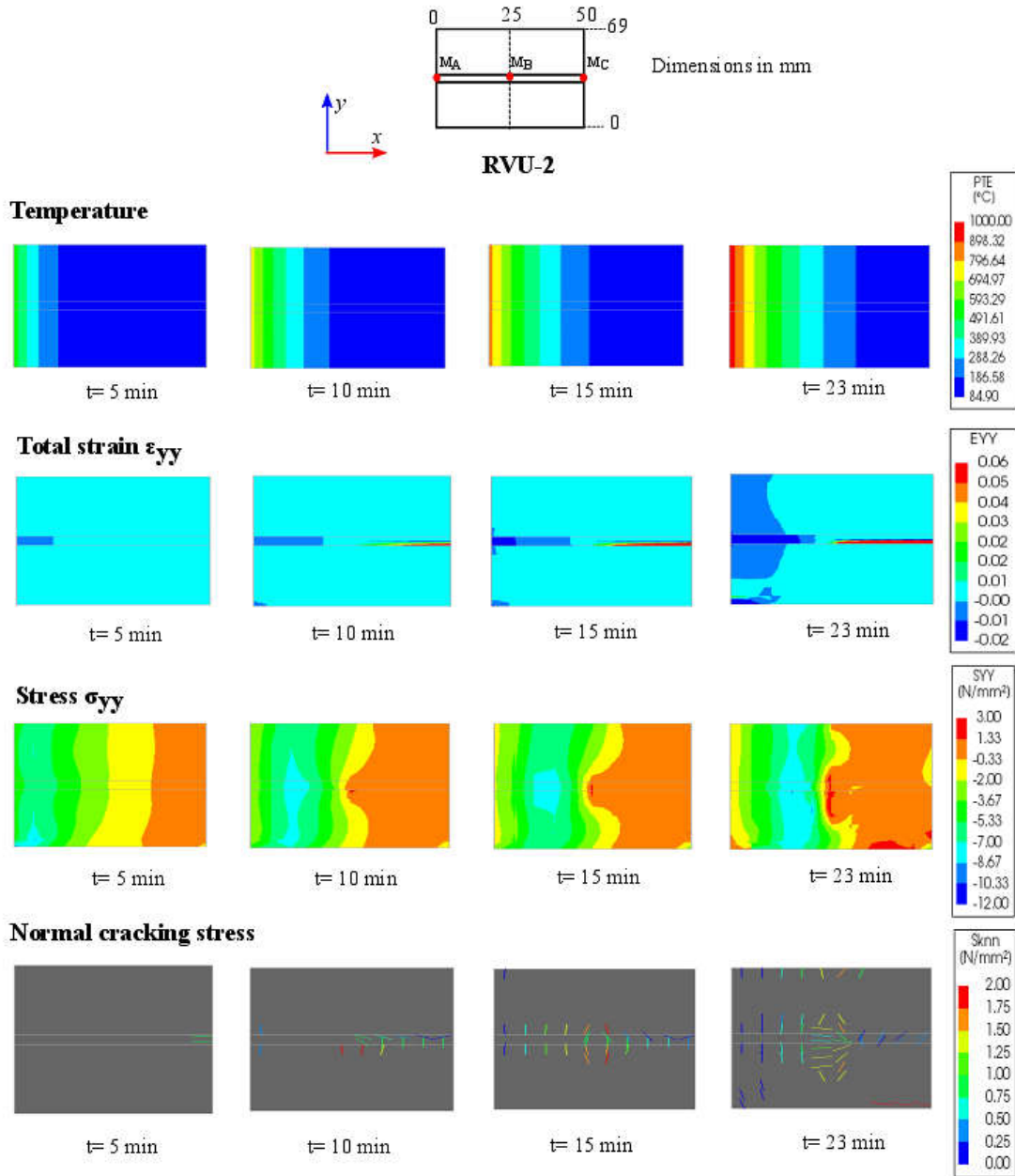
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645 **Figure 13: Thermo-mechanical response history of RVU-1 (half-scale masonry wall at 0.66**

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m from base).

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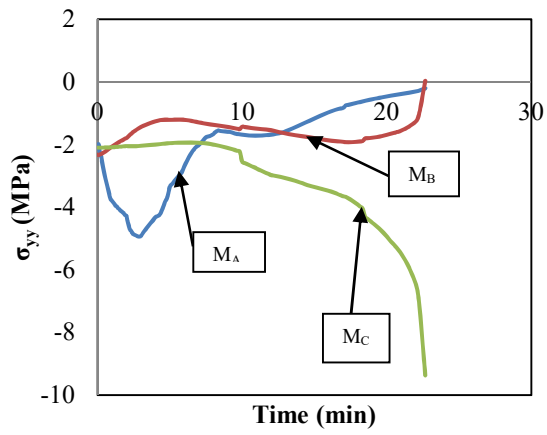


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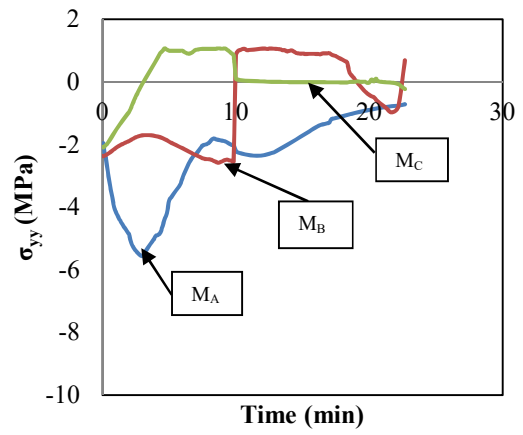
650 **Figure 14: Thermo-mechanical response history of RVU-2 (half-scale masonry wall at 0 m**
 651 **form base).**

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a) RVU-1

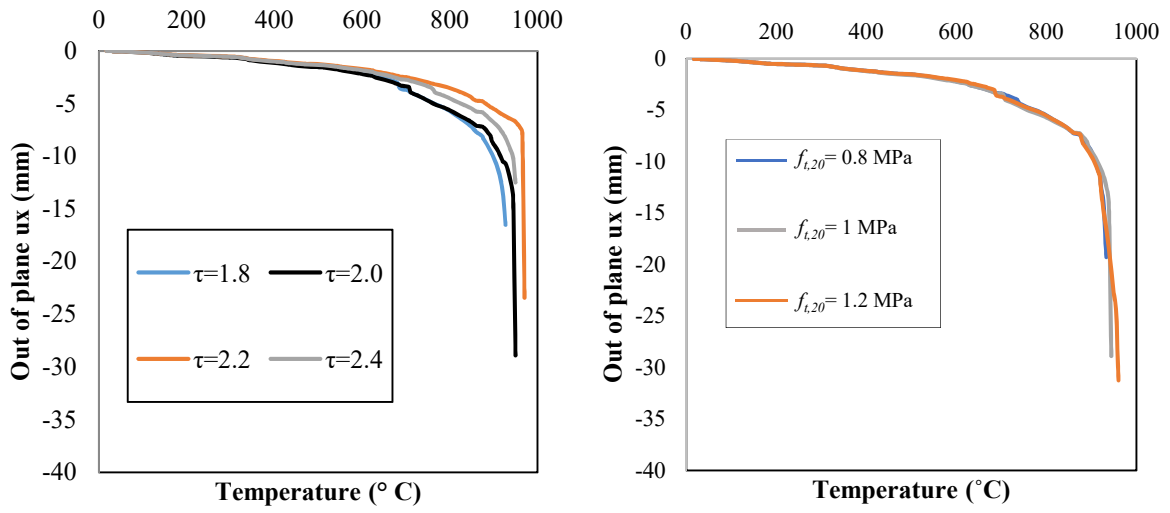


b) RVU-2

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Figure 15: Stress states in RVU-1 and RVU-2 of the half-scale masonry wall.

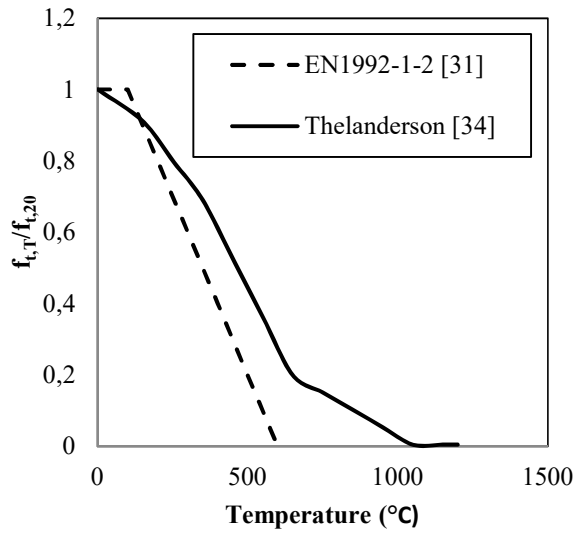
655



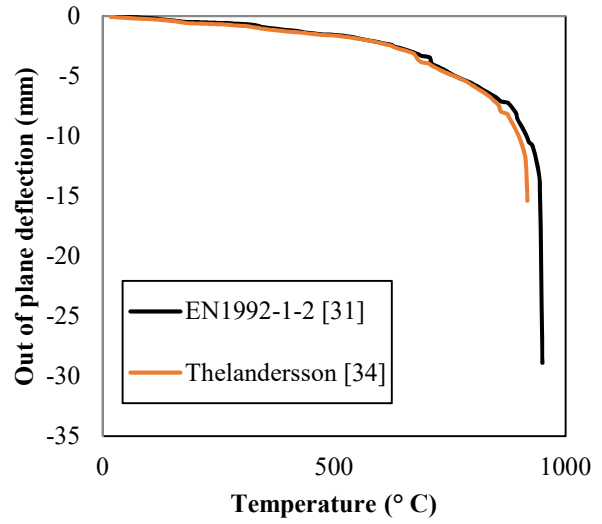
a) Effect of Transient creep

b) Effect of tensile strength of mortar

Figure 16: Parametric studies on transient creep and tensile strength of mortar.



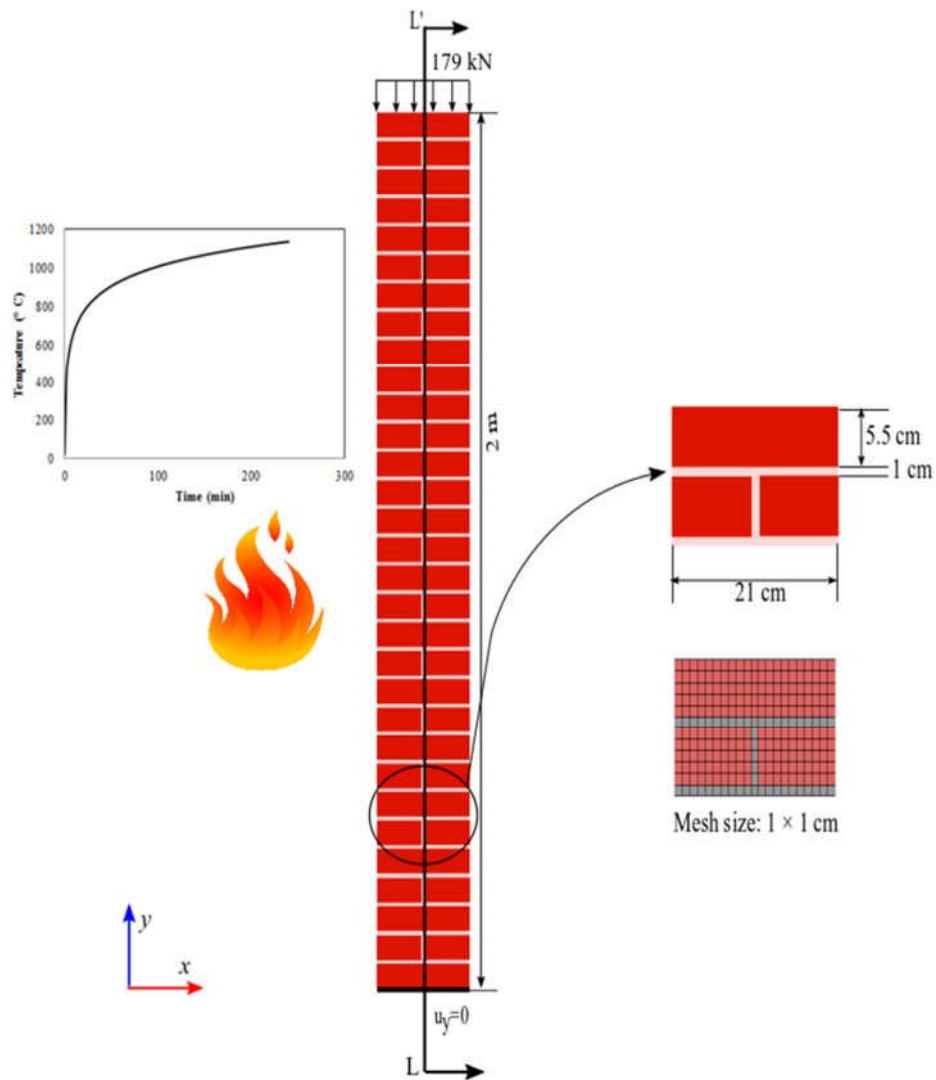
a) Temperature-dependency in tensile strength



b) Effect of temperature-dependency in concrete unit and cement mortar

660 **Figure 17: Parametric studies on temperature-dependency of concrete unit and cement**
 661 **mortar.**

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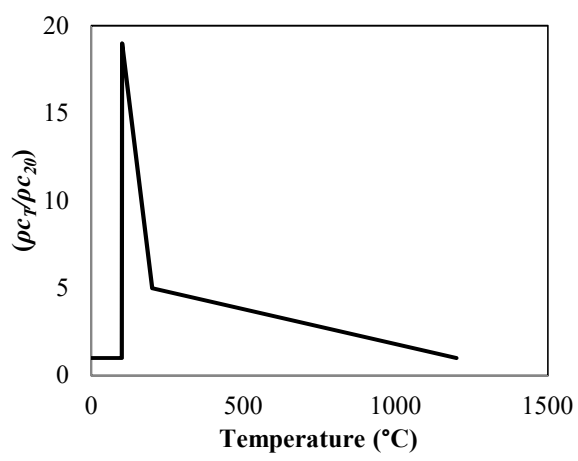
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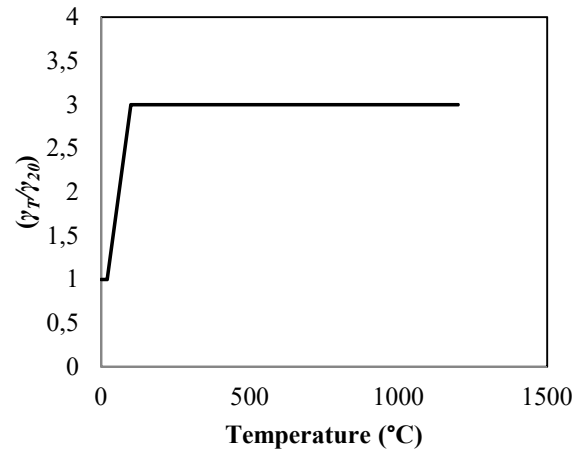
Figure 18: Full-scale masonry wall subjected to standard fire exposure.

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a) Specific-heat capacity



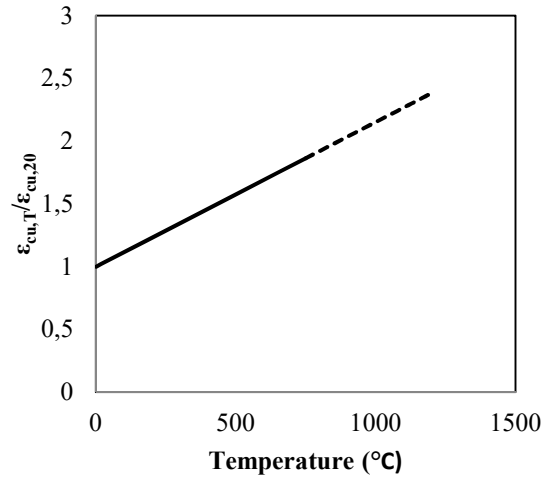
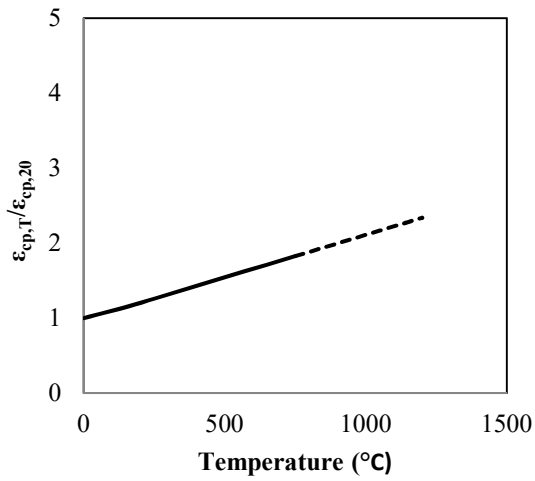
b) Thermal-conductivity

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Figure 19: Temperature-dependent thermal properties of clay unit.

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a) Strain at peak compressive strength ($\epsilon_{cp,T}$)

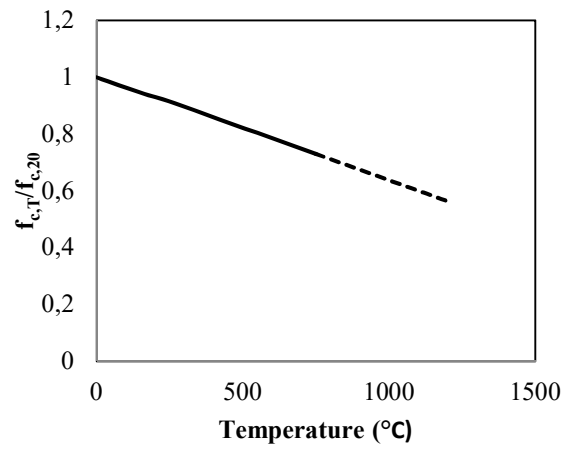
b) Ultimate compressive strain ($\epsilon_{cu,T}$)

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Figure 20: Temperature-dependent $\epsilon_{cp,T}$ and $\epsilon_{cu,T}$ in clay unit.

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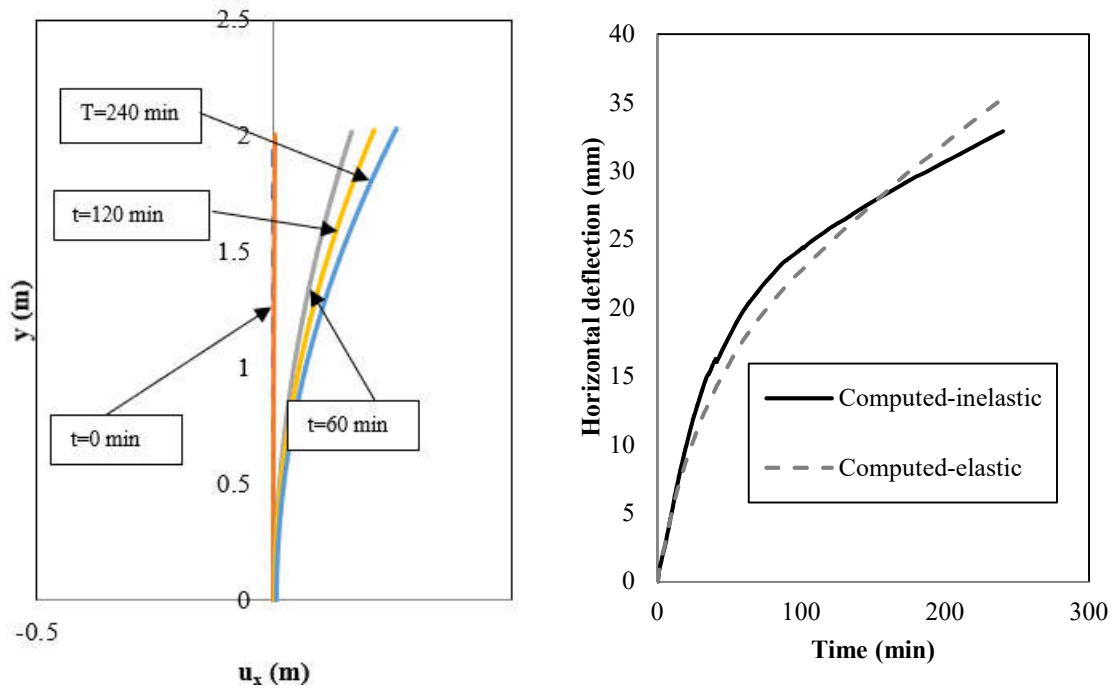
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Figure 21: Temperature-dependent compressive strength of clay unit.

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a) Deformed configuration of the central line

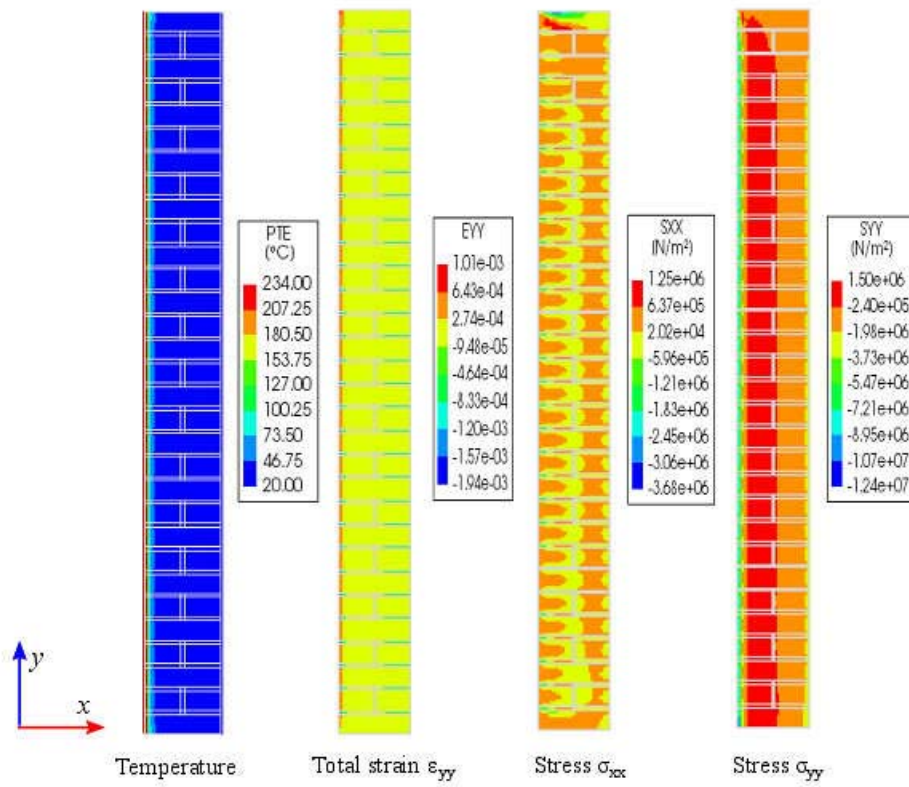
b) Deformation history at the top of the masonry wall

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Figure 22: Deformed mechanical response of full-scale wall (Scaling 10x).

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Figure 23: Thermo-mechanical response of full-scale masonry wall at $t=5$ min.

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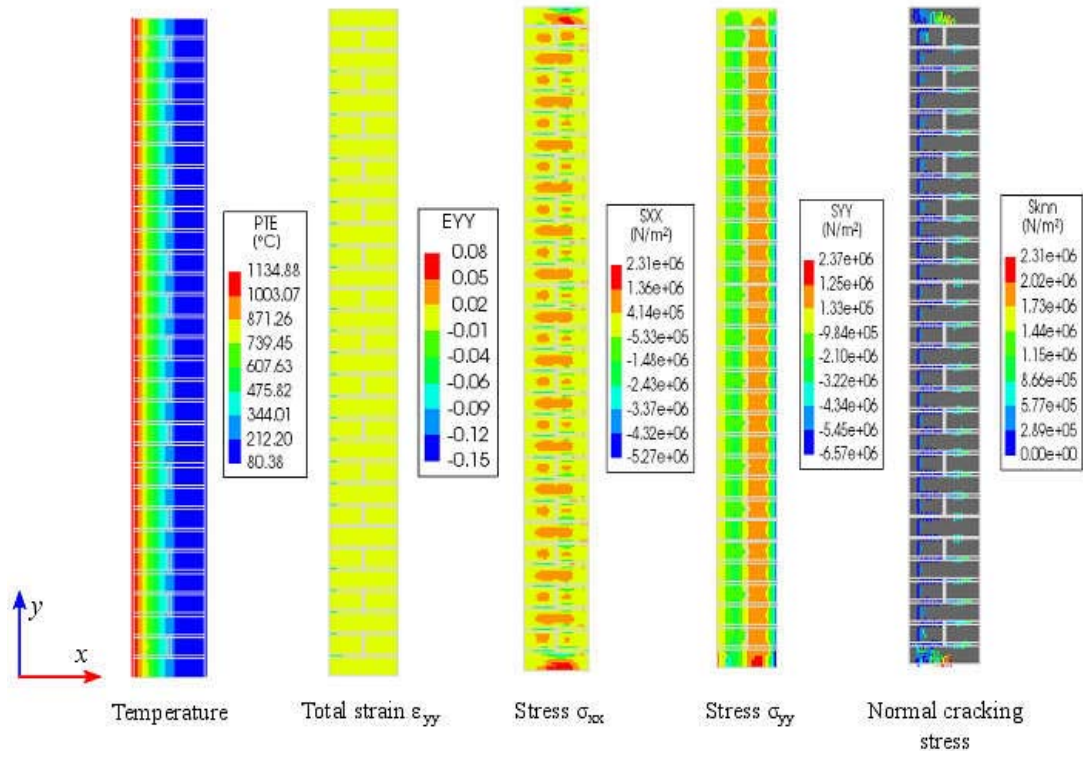
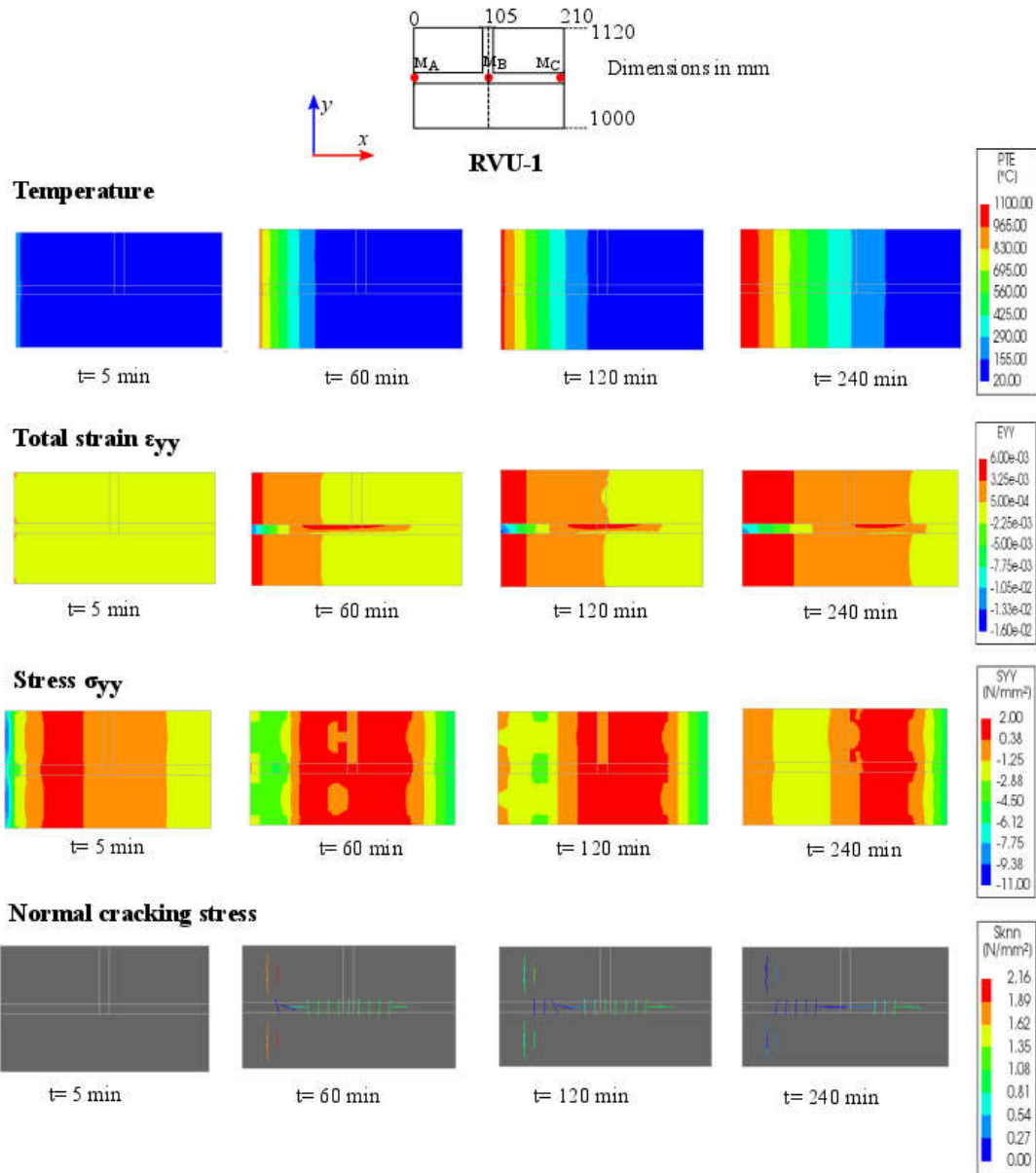


Figure 24: Thermo-mechanical response of full-scale masonry wall at $t=240$ min.

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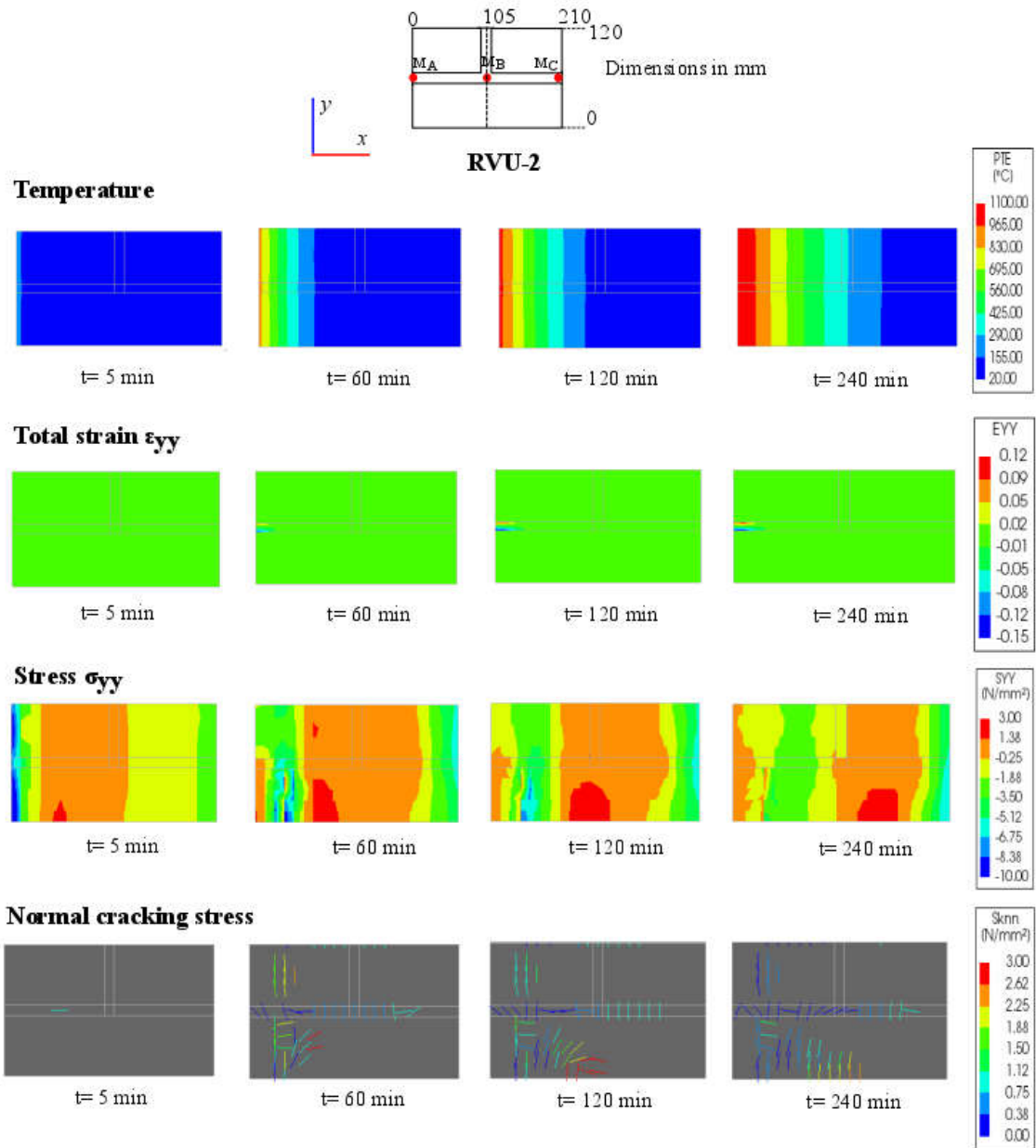
689

690 **Figure 25: Thermo-mechanical response history of RVU-1 (full-scale masonry wall at 1 m**

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from base).

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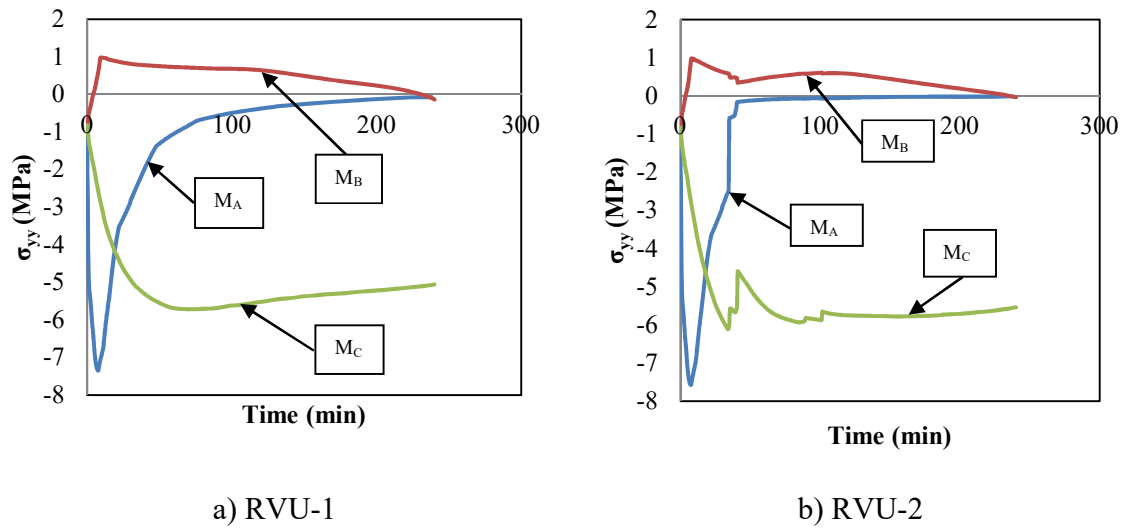


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695 **Figure 26: Thermo-mechanical response history of RVU-2 (full-scale masonry wall at 0 m**
 696 **from base).**

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Figure 27: Stress states in RVU-1 and RVU-2 of the full-scale masonry wall.

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