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Selective Harmonic Measurement and Compensation Using Smart Inverters in a Microgrid with Distributed Generation

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Abstract—This paper presents a frequency domain selective harmonic measurement and compensation using smart inverters (SIs) applied to a microgrid with distributed generation. The compensation current is calculated by a main processing unit (MPU), which controls the compensation action of each distributed generation unit (DGU) connected to the microgrid. A single fast Fourier transform (FFT) is implemented to obtain the frequency spectra of the power grid voltages and the currents consumed by the connected loads. Based on the calculated compensation currents and the availability of the DGUs, the MPU establishes the harmonic orders that each DGU should compensate, aiming to equalize the rms current values among the different DGUs. The proposed approach intends to optimize the DGUs efficiency in the microgrid and, additionally, it allows the connection of the converters to the power grid without the need for a synchronization algorithm. A comprehensive description of the implemented FFT algorithm is performed and, finally, the operation of the proposed scheme is verified by simulation results.

Keywords—Microgrid, Distributed Control Systems, Selective Harmonic Compensation, Fast Fourier Transform (FFT).

I. INTRODUCTION

Renewable energy sources (RESs) perform a continuously growing role in the present industrialized society, as they contribute to reduce greenhouse gasses emissions and to alleviate the extraction of the pollutant, nonrenewable fossil fuels [1]. Moreover, the integration of RESs in the power grid provides load support during higher demand periods, whereby distributed generation appears as an imminent trend in contrast with the traditional centralized distribution [2][3]. Among the existing types of RESs, wind and solar photovoltaic (PV) represent the main propensity [4][5].

However, RESs are characterized by their intermittence. Reference [6] analyzes the variability and uncertainty of PV energy and management strategies to be considered towards its integration in the power grid. In order to handle the distributed generation intermittence, energy storage systems (ESSs) have a vital role, emerging as a key concern in the future power grids [7]. An economic evaluation of ESSs in a context of RESs is presented in [8], in which the benefits of the former were verified. Besides the problem of intermittence, the interface of RESs with the power grid can origin power quality problems, such as voltage sags and frequency deviations. Being a crucial aspect for the stability of the power grid, power quality must be taken into consideration towards the integration of RESs [9].

As a result of the growing concerns about distributed generation, the paradigms of microgrids and smart grids have emerged and gained attention over the last years [10][11][12], in which power electronics undergoes an essential involvement [13]. Concerning microgrids, these can operate either in islanded mode or in grid-connected mode. Power control strategies for microgrids are investigated in [14] and [15] for islanded operation and in [16] for grid-connected operation. Optimal control strategies from the ESSs point of view can also be considered as presented in [17]. Besides the operation modes, microgrids can be classified accordingly with the type of power, i.e., ac or dc. Dc microgrids are a suitable approach provided that most modern loads rely on dc power, therefore it is possible to eliminate the typical ac-dc conversion and its respective power losses [18]. However, a high-frequency ac approach also offers advantages when compared to traditional line-frequency microgrids [19]. A hybrid microgrid is proposed in [20], addressing the benefits of both ac and dc power.

Power quality issues in microgrids have also been an object of investigation [21]. The compensation of power quality problems is scrutinized in [22], for three-phase four-wire microgrids, and in [23] for high-frequency ac microgrids. Basically, the referred compensators are active power filters of both series and shunt type. Regarding shunt active power filters (SAPFs), the last decades have experienced a considerable research in both hardware topologies and control systems [24]. Several power theories for SAPFs have been proposed and developed, e.g., instantaneous reactive power theory (also called $p-q$ theory) [25], Fryze-Buchholz-Depenbrock power theory [26], current's physical components power theory [27] and synchronous reference frame $(d-q)$ power theory [28]. Among the investigated and proposed theories, time domain power theories are mostly preferred due to the provided fast response and relatively low computational cost. However, the time domain approach is ineffective (and can be even aggravative) towards resonance conditions in the power grid. Harmonic interaction in a context of RESs-based distributed generation is investigated in [29], while [30] and [31] focus on resonance damping in islanded microgrids.

On the other hand, a frequency domain approach allows an individually harmonic measurement, therefore permitting a selective harmonic compensation [32]. Frequency domain power theories apply Fourier analysis, with the fast Fourier transform (FFT) being considered the most efficient class of algorithms to perform such analysis [33]. Nevertheless, FFT calculations require higher computational costs than time

domain power theories, whereby frequency selective filters can be employed instead [34]. However, this method uses bandpass and bandstop filters that cannot inherently provide satisfactory attenuation without sacrificing the neighbor frequencies, which are narrowly spaced considering power system harmonics.

Besides the compensation domain method, distributed or centralized approaches can be considered. A distributed system of SAPFs was initially proposed in [35], and in [36] is studied the distributed harmonic compensation in a microgrid context. A cooperative control of SAPFs is investigated in [37], in which are presented better results than independent control in terms of harmonic damping. Considering the ongoing necessity of distributed generation and the microgrid paradigm, distributed power quality conditioning is an impending approach for future power grids.

Thereupon, taken into consideration the referred aspects, this paper presents a selective harmonic measurement and compensation using smart inverters (SIs) for a single-phase RESs-based microgrid, where the several connected distributed generation units (DGUs) operate as SAPFs in a distributed manner. A single FFT algorithm is implemented by a main processing unit (MPU) to extract the harmonic content of both power grid voltage and loads current, therefore discarding the use of a synchronization mechanism with the power grid. The MPU evaluates the power availability of each DGU and, as a function of such assessment, defines the harmonic order to be compensated.

The paper is structured as follows: Section II presents the structure of the microgrid from the MPU and DGUs perspective; Section III describes the reference current generation for the SAPF operation, presenting a comprehensive analysis of the implemented FFT algorithm; Section IV depicts the obtained simulation results for the distributed compensation system; lastly, Section V outlines the main conclusions of the investigation carried out.

II. MICROGRID STRUCTURE

This section presents the structure of the DGUs comprising the microgrid, as well as the processing performed by the MPU. A single-line diagram of the microgrid constitution is presented in Fig. 1, where several DGUs, comprised by the respective SI and RES, and different connected loads can be seen. As it can be noticeable, the microgrid is of the grid-connected type.

A. Distributed Generation Units (DGUs)

Each DGU is comprised by a SI, i.e., a dc-ac power converter connected to the microgrid, and dc-dc and/or ac-dc power converters interfacing the RES with the previously referred converter, depending on the used RES. As it can be seen in Fig. 1, both PV and wind power are considered, whereby the dc-dc and/or ac-dc set of power converters operate with the purpose of extracting the maximum power of the RES available at each instant. In the scope of this paper, the power converter topologies are not scrutinized, as well as the operation of the RESs interfacing converters. Therefore, only the operation of the SIs is analyzed from the DGUs point of view. It should be referred that the SIs operate in a current-control scheme, allowing the injection of the extracted energy into the microgrid and, simultaneously, the SAPF operation. Regarding the energy injection, each DGU produces a line-frequency sinusoidal

Fig. 1. Structure of the distributed microgrid with n DGUs, the respective RESs and x connected loads.

current with a 180º phase difference from the grid voltage so that it operates as a power source, aiming for a practically unitary power factor. Considering the SAPF operation, the reference current in the time domain is wirelessly transmitted by the MPU, whereby each DGU must accommodate both current components (fundamental plus harmonics) in its synthesized current so that the two tasks can be properly accomplished.

B. Main Processing Unit (MPU)

As aforementioned, the MPU calculates the compensation current in the frequency domain. Besides, the MPU monitors the energy injection of each DGU in the microgrid. Since the SAPF operation does not exchange active power with the grid, the harmonic order assignment for each DGU focuses on balancing the rms current along the different DGUs. Afterwards, the MPU communicates the grid voltage and the reference current in the time domain to each DGU, whereby the latter adjusts its total reference current to perform the energy injection into the power grid while compensating the given harmonics.

III. REFERENCE CURRENT GENERATION

In this section, the details associated to the calculation of the reference current for the SAPF operation of each DGU are examined. The reference current is attained with a frequency domain method, namely via a complex FFT. Having a high computational burden, the FFT is calculated by the MPU, which commands the operation of the connected DGUs.

A. Real FFT versus Complex FFT

FFT algorithms are an efficient way of calculating the discrete Fourier transform (DFT). These algorithms can be classified between two types regarding the applied input data: real FFT and complex FFT. The former is appropriate provided that any measured signal in a power system is a real number, whereby this algorithm operates with real numbers, increasing the algorithm computational speed. On the other hand, the complex FFT uses complex numbers as its input data. Although the complex FFT can be used with real numbered inputs, i.e., by setting the input imaginary part to zero, it is less efficient than the real FFT; in fact, the real FFT is an optimized version of the complex FFT for real signals.

However, the complex FFT allows a useful feature towards real signals. Instead of being null, the input imaginary part can be used to place a second real numbered input signal, meaning

Fig. 2. Dual input complex FFT calculation: (a) Nonlinear load current (i_{ld}) and (b) power grid voltage (v_g) used as FFT inputs; (c) Real part (Re{Z[k]}) and (d) Imaginary part $(\text{Im}\{Z[k]\})$ of the FFT of $z[n]$; (e) Real part $(\text{Re}\{I_{ld}[k]\})$ and (f) Imaginary part $(\text{Im}\{I_{ld}[k]\})$ of the FFT of $i_{ld}[n]$; (g) Real part $(\text{Re}\{V_g[k]\})$ and (h) Imaginary part (Im $\{V_g[k]\}$) of the FFT of $v_g[n]$.

that a single FFT can be applied for two different signals. This is possible due to the existing even and odd symmetries in the frequency spectrum of a signal. Once calculated, the frequency spectrum can be separated in its even and odd parts, allowing the construction of two different spectra that correspond to the individual FFTs of both input signals. This technique allows a processing time reduction of almost a half if more than one signal is intended to be analyzed by an FFT algorithm [38].

B. Complex FFT with Two Input Signals

As aforementioned, a single complex FFT can be employed to determine the spectra of two real signals. Fig. 2 (a) and Fig. 2 (b) show two distorted power signals, namely a current absorbed by a single-phase diode bridge rectifier with capacitive output filter (i_{ld}) and the respective supplied voltage (v_g) . From both signals, and considering a discrete time implementation, a complex signal $z[n]$ can be assembled. Considering i_{ld} as the real part and v_g as the imaginary part, the discrete time domain complex signal $z[n]$ can be attained in accordance with: *z* network the complex FFT can be employed

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termine the spectra of two real signals, namely a current

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$$
z[n] = i_{ld}[n] + j v_g[n], \qquad (1)
$$

where *j* represents the complex variable. It should be noted that $z[n]$ is deprived of physical meaning. Afterwards, the time domain signal $z[n]$ can be transposed to the frequency domain by means of the complex FFT, yielding $Z[k]$:

$$
Z[k] = FFT(z[n]) = \text{Re}\{Z[k]\} + j\ \text{Im}\{Z[k]\},\tag{2}
$$

where k is the discrete frequency index, whose value varies between 0 and N-1, with N being the FFT number of points, and $\text{Re}\{Z[k]\}\$ and $\text{Im}\{Z[k]\}\$ are the real and imaginary parts of the compound $Z[k]$ spectrum, respectively. Both components are shown in Fig. 2 (c) and Fig. 2 (d) and satisfy the following: Example the privarial meaning. Afterwards, the time

ignal $z[n]$ can be transposed to the frequency domain

it of the complex FFT, yielding $Z[k]$:
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is the discrete freq of the complex FFT, yielding $Z[k]$:
 $E:]=FFT(z[n]) = \text{Re}\{Z[k]\} + j \text{Im}\{Z[k]\},$ (2) in

is the discrete frequency index, whose value varies
 E and $N-1$, with N being the FFT number of points, and

and $\text{Im}\{Z[k]\}$ are the real

$$
\operatorname{Re}\left\{Z[k]\right\} = \operatorname{Re}\left\{I_{ld}[k]\right\} + j \operatorname{Im}\left\{V_g[k]\right\} \tag{3}
$$

$$
\operatorname{Im} \{Z[k]\} = \operatorname{Re}\{V_g[k]\} + j \operatorname{Im}\{I_{ld}[k]\} \tag{4}
$$

The objective is to separate each spectrum in order to attain the two spectra $I_{ld}[k]$ and $V_{g}[k]$. As previously referred in this section, the feasibility of a dual input single FFT relies on the symmetry properties of the frequency domain. For a single, purely real input FFT, the real part of the frequency domain presents an even symmetry around the sample N/2, while the imaginary part has odd symmetry. Thus, the following relationships are valid for $k > 0$ and $k < N$:

$$
\operatorname{Re}\{Z[k]\} = \operatorname{Re}\{Z[N-k]\}\tag{5}
$$

$$
\text{Im}\{Z[k]\} = -\text{Im}\{Z[N-k]\}\tag{6}
$$

In a dual input FFT, both types of symmetry are present in the real and imaginary parts. According to (3), $\text{Re}\{I_{ld}[k]\}\)$ can be extracted by cancelling $\text{Im}\{V_{\rho}[k]\}\$, which is possible due to the odd symmetry of the latter. Similarly, $Im{I_{ld}[k]} can be attained$ from (4) by cancelling $\text{Re}\{V_g[k]\}\$ due to its even symmetry. These operations are performed by the following: Im { $Z[k]$ } = - Im { $Z[1N - k]$ }
dual input FFT, both types of symmetry are preseend
and imaginary parts. According to (3), Re { $I_{ld}[k]$ } can
by cancelling Im { $V_g[k]$ }, which is possible due to
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c]} = - Im { $Z[N - k]$ (6)

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arts. According to (3), Re { $I_{l,d}[k]$ } can be

Im { $V_g[k]$ }, which is possible due to the

ter. Similarly, Im { $I_{l,d}[k]$ } can be atta and imaginary parts. According to (3), $\kappa \in \{I_d[n]\}$ ed
d by cancelling Im $\{V_g[k]\}$, which is possible due to
metry of the latter. Similarly, Im $\{I_{id}[k]\}$ can be atta
(b) by cancelling $\text{Re}\{V_g[k]\}$ due to its even symm If $I = \text{Im}\{Z\{N - k\}}$ (0)

S, both types of symmetry are present in

parts. According to (3), Re { $I_{ld}[k]$ } can be

Im $\{V_g[k]\}$, which is possible due to the

tter. Similarly, Im $\{I_{ld}[k]\}$ can be attained
 $\{Re\{V_g[k]\}$ d

$$
Re{I_{ld}[k]} = \frac{Re{Z[k]} + Re{Z[N-k]}}{2}
$$
 (7)

Im
$$
\{I_{ld}[k]\} = \frac{\text{Im}\{Z[k]\} - \text{Im}\{Z[N-k]\}}{2}
$$
, (8)

whose spectra are presented in Fig. 2 (e) and in Fig. 2 (f), respectively.

For obtaining $V_g[k]$, similar operations are used. However, since the time domain signal v_{ϱ} was introduced as an imaginary argument of a complex number, the corresponding spectrum will appear multiplied by j , i.e., shifted by 90° . Therefore, instead of cancelling the even component of Re $\{Z[k]\}$ to obtain Re $\{V_g[k]\},$ it is necessary to cancel the odd component of $Im{Z[k]}$. Likewise, instead of cancelling the odd component of $Im{Z[k]}$ in order to obtain $\text{Im}\{V_g[k]\}$, it is necessary to cancel the even part of $\text{Re}\{Z[k]\}$ and negate the obtained result. This procedure corresponds to a multiplication by $-j$ (which is a 90 \degree clockwise rotation) and it is mandatory to be performed in order to obtain the correct phase angles for the frequency components of v_g . The real and imaginary components of $V_g[k]$ are depicted in Fig. 2 (g) and Fig. 2 (h) and are attained according with: e, instead of $V_g[k]$, it is necessary to cancel the
to obtain Im{ $V_g[k]$,} it is necessary to cancel the
 $Re\{Z[k]\}$ and negate the obtained result. This proce
onds to a multiplication by $-j$ (which is a 90° clock)
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 $S_g[k]$,} it is necessary to cancel the even
gate the obtained result. This procedure
lication by $-j$ (w ond it is mandatory by $-y$ (which is a 50 clock
) and it is mandatory to be performed in order to c
cet phase angles for the frequency components of v_g
d imaginary components of $V_g[k]$ are depicte
g) and Fig. 2 (h) and [g[k],} it is necessary to cancel the even
gate the obtained result. This procedure
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tory to be performed in order to obtain
for the frequency components of v_g . The
omponents of

$$
\operatorname{Re}\{V_g[k]\} = \frac{\operatorname{Im}\{Z[k]\} + \operatorname{Im}\{Z[N-k]\}}{2} \tag{9}
$$

Im
$$
\{V_g[k]\} = \frac{\text{Re}\{Z[N-k]\} - \text{Re}\{Z[k]\}}{2}
$$
 (10)

Once obtained the two separated spectra, it is convenient to transform the rectangular coordinates into polar coordinates, therefore obtaining a value of amplitude and phase for each measured frequency. For a given index k of the frequency spectrum of i_{ld} , the corresponding amplitude $(A_{\text{Id}}[k])$ and phase $(\theta_{\text{Ild}}[k])$ can be attained in conformity with:

$$
A_{I_d}[k] = \sqrt{\text{Re}\{I_{ld}[k]\}^2 + \text{Im}\{I_{ld}[k]\}^2}
$$
(11)

$$
A_{I_d}[k] = \sqrt{\text{Re}\{I_{ld}[k]\}^2 + \text{Im}\{I_{ld}[k]\}^2}
$$
 (11)
\n
$$
\theta_{I_d}[k] = \arctan\left(\frac{\text{Im}\{I_{ld}[k]\}}{\text{Re}\{I_{ld}[k]\}}\right)
$$
 (12)
\nse angle of the fundamental component of the power
\ni is the reference for all phase angles for both voltage

The phase angle of the fundamental component of the power grid voltage is the reference for all phase angles for both voltage and current. However, since the algorithm is devoid of synchronization, the calculated phase angle for the power grid voltage fundamental component (θ_0) is used in the calculations of all remaining angles, making it possible to establish the former as the referential phase. Therefore, for each frequency k , the phase angle of its current component (θ_{Ild}) will be calculated with respect to θ_0 .

After obtaining the values of amplitude and phase of each detected frequency for the load current, the control system is capable of generating a reference current for the SAPF operation of the DGUs in a harmonic selective manner. To compensate a given harmonic, the reference current should contain an equal amplitude and a 180º phase difference to those of the desired harmonic. However, in order to compensate for fundamental reactive power, a different scheme must be applied. Since it is desirable for the power grid to supply only active power to the loads, the DGUs must supply the required reactive power. In the frequency spectrum, this means that the power grid must supply the real part of the fundamental current ($\text{Re}\{I_{ld}[1]\}$), meaning that the compensation current should contain only $\text{Im}\left\{I_{ld}[1]\right\}$, where $k = 1$ refers to the fundamental frequency. However, the real and imaginary fundamental current components cannot be used directly because of θ_0 , since the absolute zero phase coincides with the initial instant of the control algorithm. In this context, the real and imaginary components of the compensation current can be properly attained by means of the following: DGUs must supply the required reactive power. In the

v spectrum, this means that the power grid must supply

be evaluated

and of the fundamental current (Re { $I_{ld}[1]$ }), meaning

compensation current should contain only by the fundamental current (Re { $I_{ld}[1]$ }), meaning points (N). I
compensation current should contain only Im { $I_{ld}[1]$ }, frequency, v
= 1 refers to the fundamental frequency. However, the to the numb
imaginary fundamenta

$$
\operatorname{Re}\{I_{\text{ref}}[1]\}=A_{I_{\text{td}}}[1]\sin(\theta_{I_{\text{td}}}[1])\sin(\theta_0) \qquad (13)
$$

Im
$$
\{I_{ref}[1]\}=A_{I_d}[1]sin(\theta_{I_d}[1])cos(\theta_0),
$$
 (14)

where $\theta_{\text{I} \text{d}d}[1]$ is the phase difference between the fundamental components of i_{ld} and v_g . Fig. 3 shows a phasor diagram illustrating the referred calculations for the fundamental frequency, where can be seen the load current (I_{ld}) , the power grid voltage (\dot{V}_g), the phase angle of the power grid voltage with respect to the FFT algorithm starting (θ_0) , the phase difference between the voltage and current (θ_{Ild}), the reference current for the SAPF operation (I_{ref}) and the corresponding real and imaginary components (Re ${I_{ref}}$ and Im ${I_{ref}}$, respectively). It should be noted that this approach dismisses the need of a synchronization algorithm (e.g., phase-locked loop) with the power grid at the expense of an almost negligible extra computation in the FFT algorithm.

IV. SIMULATION RESULTS

This section presents the simulation results of the developed compensation scheme for the RESs-based distributed microgrid. The computational simulations were performed with the software PSIM v9.1 from PowerSim.

Fig. 3. Phasor diagram representing the calculation of the reference current fundamental component (I_{ref}) for the SAPF operation.

A. System Parameters

As referred in Section II, the inner constitution of the DGUs is not discriminated in this paper. Accordingly, the considered power system parameters are the power grid nominal voltage and frequency (230 V, 50 Hz) and the power rating of each DGU, for which a value of 3 kW (corresponding to a maximum rms current of 13 A) was established.

Concerning the FFT algorithm, two main parameters should be evaluated: the sampling frequency (F_s) and the number of points (N). The first parameter defines the maximum measurable frequency, which is $F_s/2$. On the other hand, N is directly related to the number of measurable frequencies, which is N/2. In order to define the spectral resolution of the FFT, both parameters must be selected in consonance. Considering that the microgrid is connected to a power grid with a fundamental frequency of 50 Hz, the desired spectral resolution was chosen to be 50 Hz, which also defines this value as the lowest detectable frequency. Since the spectral resolution is given by F_s/N and the optimal values of N in an FFT are powers of two, F_s should be selected accordingly. The maximum measurable frequency was chosen to be between 10 kHz and 20 kHz, whereby the closest value is attained with $N = 512$ and $F_s = 25.6$ kHz, which provides a maximum frequency of 12.8 kHz to be measured.

B. Microgrid Operation

Fig. 4 depicts the operation of four DGUs both before and after the compensation is activated. In the beginning (from 0.02 s to 0.1 s) the compensation scheme is disabled, whereby the DGUs operate with the purpose of injecting energy into the microgrid. As it can be seen in the referred time interval, the current produced by each DGU (i DGU₁, i DGU₂, i DGU₃, i DGU₄) is sinusoidal (with a frequency equal to the line-frequency) and in opposite phase with the grid voltage (v_g) , showing the contribution of the DGUs to the microgrid. Moreover, the injected currents are insensitive to the distortion of v_g . It is also noticeable that the DGUs present dissimilar rms current values. On the other hand, the grid current (i_g) is distorted because of the connection of a nonlinear load in the microgrid, which is the load presented in Fig. 2. Despite the distortion, i_g contains a large portion of fundamental component, which is a result of the combined energy injection of the DGUs. Due to the same reason, the current i_g is in opposite phase with the voltage v_g .

Fig. 4. Simulation results of the proposed scheme with four different DGUs injecting energy into the microgrid before and after performing compensation: (a) Grid voltage (v_g) and current (i_g) ; (b) Currents produced by DGU n $(i_{DGUn}$, n = {1, 2, 3, 4}).

At the instant 0.1 s the compensation is activated, therefore the DGUs start to operate with two purposes: continuing to inject the available energy and compensating the harmonic currents and/or fundamental reactive power required by the connected load. Hence, DGU #1 compensates the third harmonic (150 Hz), DGU #3 compensates the fifth harmonic (250 Hz) and DGU #4 compensates the seventh harmonic (350 Hz). On the other hand, DGU #2 does not perform harmonic compensation, producing fundamental reactive power instead. In fact, DGU #2 produces both active and reactive power, as it can be perceived by the phase angle of i_{DGU_2} , which is neither 180[°] nor -90[°]. As a result, DGU #2 provides active power to the microgrid and reactive power for compensating the displacement power factor of the connected load. It can be seen that the coordinate operation of the DGUs after instant 0.1 s is responsible for the current i_e being sinusoidal and in phase opposition with the voltage v_g .

As aforementioned, the compensation current components are assigned to each DGU as a function of its availability, i.e., in order to distribute the rms current values of each DGU. Table I shows the rms current values of each DGU before and after the compensation starting instant. As it can be noted, the smaller the rms value before the compensation, the larger the increase in the rms value after the compensation. With this strategy, the most supportive DGUs do not succumb to excessive overloads, contributing to the overall efficiency of the microgrid while compensating power quality problems in the current.

TABLE I –RMS CURRENT VALUES OF THE DGUS BEFORE AND AFTER THE COMPENSATION

BEFORE COMPENSATION	AFTER COMPENSATION		
$3.00\,\mathrm{A}$	5.90 A		
6.00 A	6.53 A		
8.00 A	8.22 A		
10.00 A	10.04 A		

V. CONCLUSIONS

A selective harmonic current compensation scheme using smart inverters (SIs) for a microgrid with distributed generation was presented. The ability to calculate the frequency spectra of two signals in a single fast Fourier transform (FFT) algorithm was demonstrated, discarding the necessity of a synchronization

mechanism with the power grid. Besides, the computational cost of calculating a dual input complex FFT is quite similar to that of a single input complex FFT. The FFT was calculated by a main processing unit (MPU), which measures the values of the grid voltages and load currents, as well as the currents injected by the several distributed generation units (DGUs) connected to the microgrid, in order to assess the availability of each one of them. Simulation results were presented to evaluate the selective harmonic compensation for four connected DGUs. It was shown that both harmonic currents and fundamental reactive power can be compensated in a selective manner by means of a single FFT algorithm. The compensation current components were shared among the different DGUs, in order to equalize the rms current of the DGUs as much as possible. With this approach, the resulting power losses within the converters were more evenly distributed along the DGUs, preventing possible malfunctions due to overloads as a consequence of dissimilar current sharing.

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